The background of the slide is a composite image. On the left, the dark, cratered surface of the Moon is visible, with the bright, curved horizon of the Earth rising from the bottom left. The right side of the image shows a deep blue space filled with numerous small white stars. A prominent bright star in the upper right quadrant has a large, multi-colored lens flare that spreads across the scene.

# **TAKING THE INVENTORY OF EXTRASOLAR PLANETS WITH MICROLENSING**

**B. Scott Gaudi**  
The Ohio State University

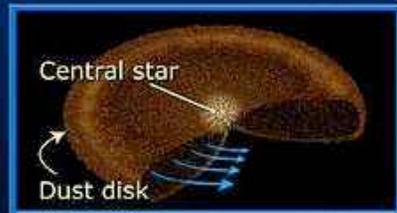
*“I don’t understand. You are looking for planets you can’t see around stars you can’t see.”*

-Debra Fischer

*“Microlensing is a cult.”*

-Dave Koerner

## Accretion model



Orbiting dust grains accrete into "planetesimals" through nongravitational forces.



Planetesimals grow, moving in near-coplanar orbits, to form "planetary embryos."



Gas-giant planets accrete gas envelopes before disk gas disappears.

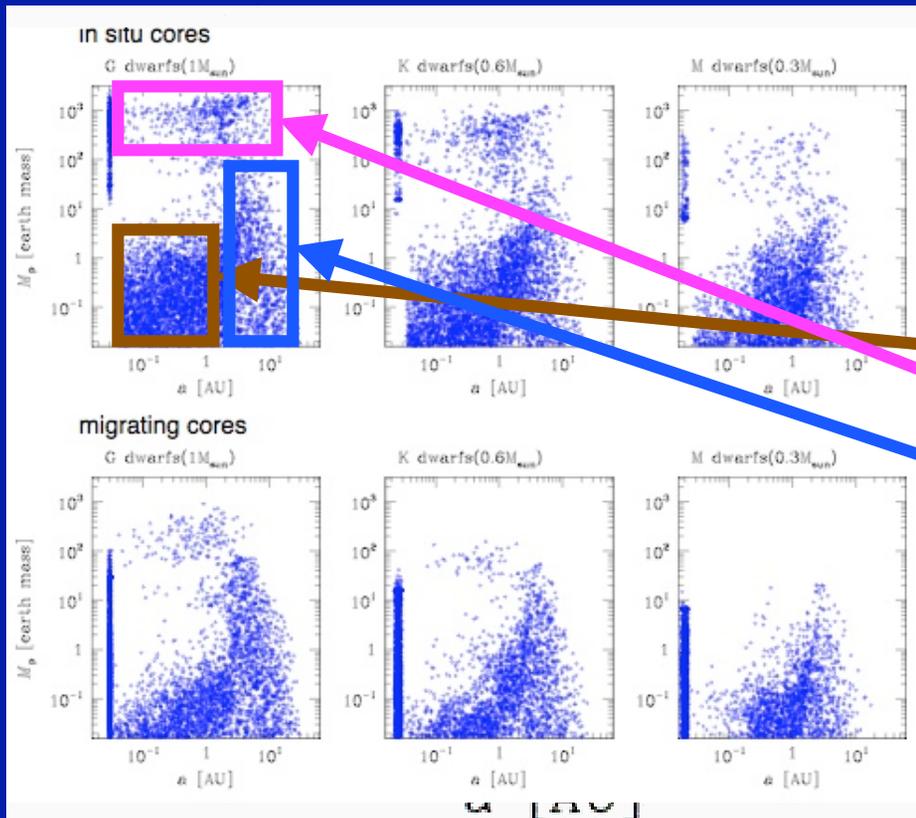


Gas-giant planets scatter or accrete remaining planetesimals and embryos.

# PLANET FORMATION

- Core-accretion Model
- Dust → Planetesimals (non G)
- Planetesimals → Protoplanets
- Protoplanets → Gas Giants (Outer Solar System)
- Protoplanets → Terrestrial Planets (Inner Solar System)

# PLANET FORMATION

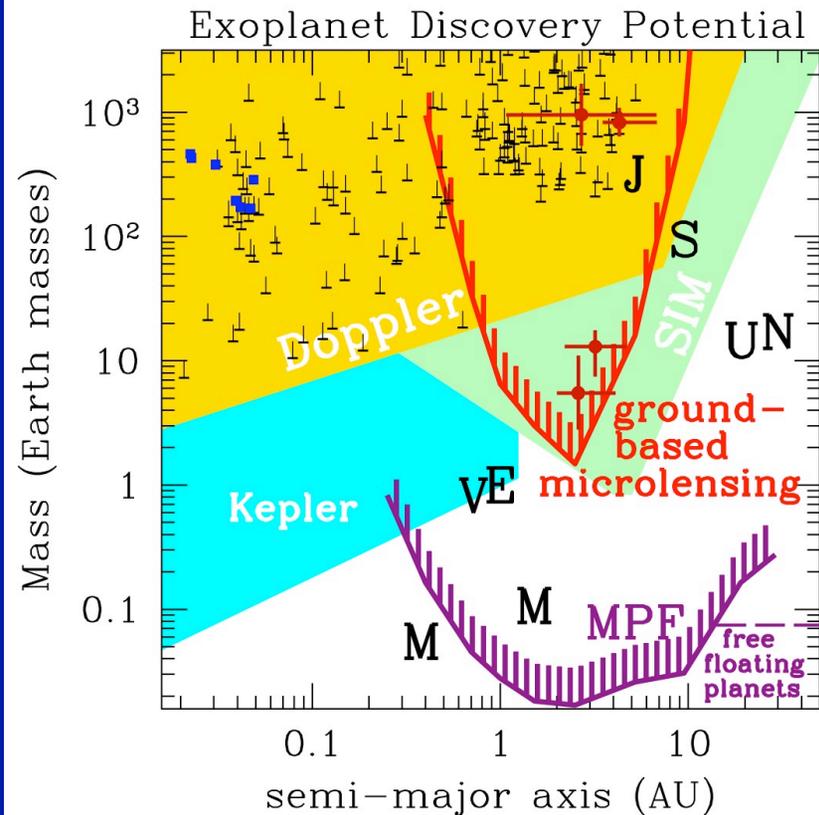
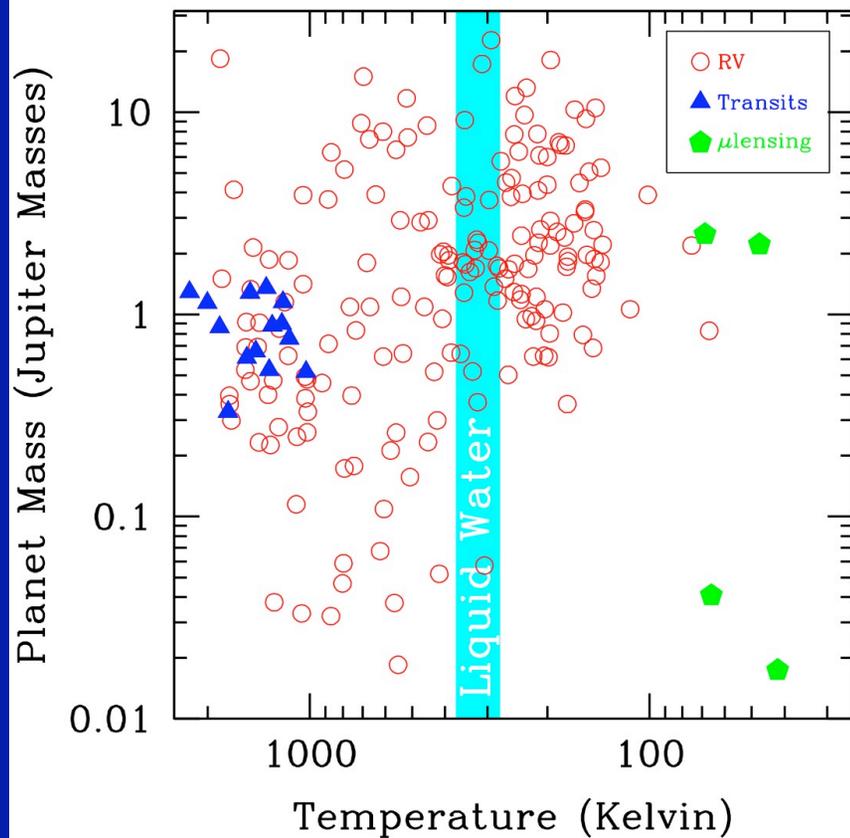


(D. Lin)

- “Semi-analytic” Planet Formation
- Three classes of planets
  - Terrestrial Planets
  - Gas Giants
  - Ice Planets
- Segregation in Mass/Separation
- Frequency versus  $M_*$  and  $M_p$

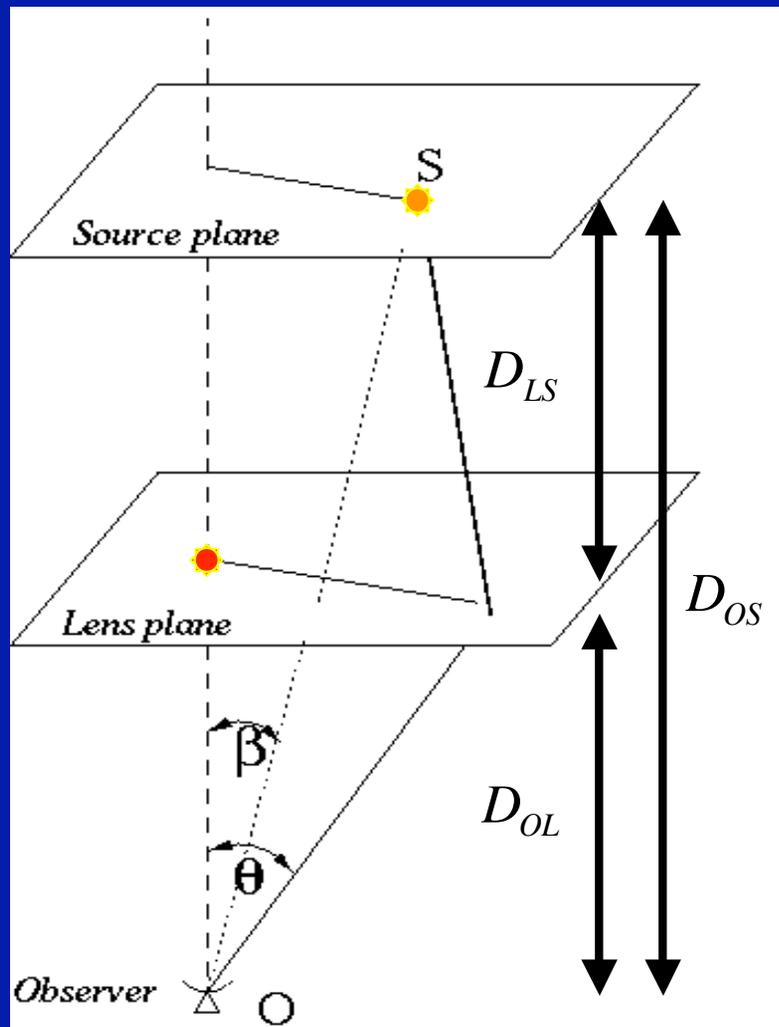
# ASSERTIONS:

- This field is observationally driven.
- Understanding planet formation requires a complete census of planets
- Issues of habitability are inexorably tied up with planet formation, and in particular processes beyond the snow line.



- Ground-based  $\mu$ lensing surveys probe low-mass planets at or beyond the snow-line.
- A space-based survey will provide a complete picture of the diversity of planetary systems for a  $> 0.5$  AU (from 0 to  $\infty$  with Kepler)
- Without  $\mu$ lensing, we will remain ignorant of many of the details of planetary systems

# GRAVITATIONAL LENSING



- Point Lens Equation

$$\beta = \theta - \theta_E^2 / \theta$$

- Einstein Ring Radius

$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_{OL}D_{OS}}}$$

$$\approx 300 \mu\text{as} \left( \frac{M}{0.3M_{\odot}} \right)^{1/2}$$

# MICROLENSING

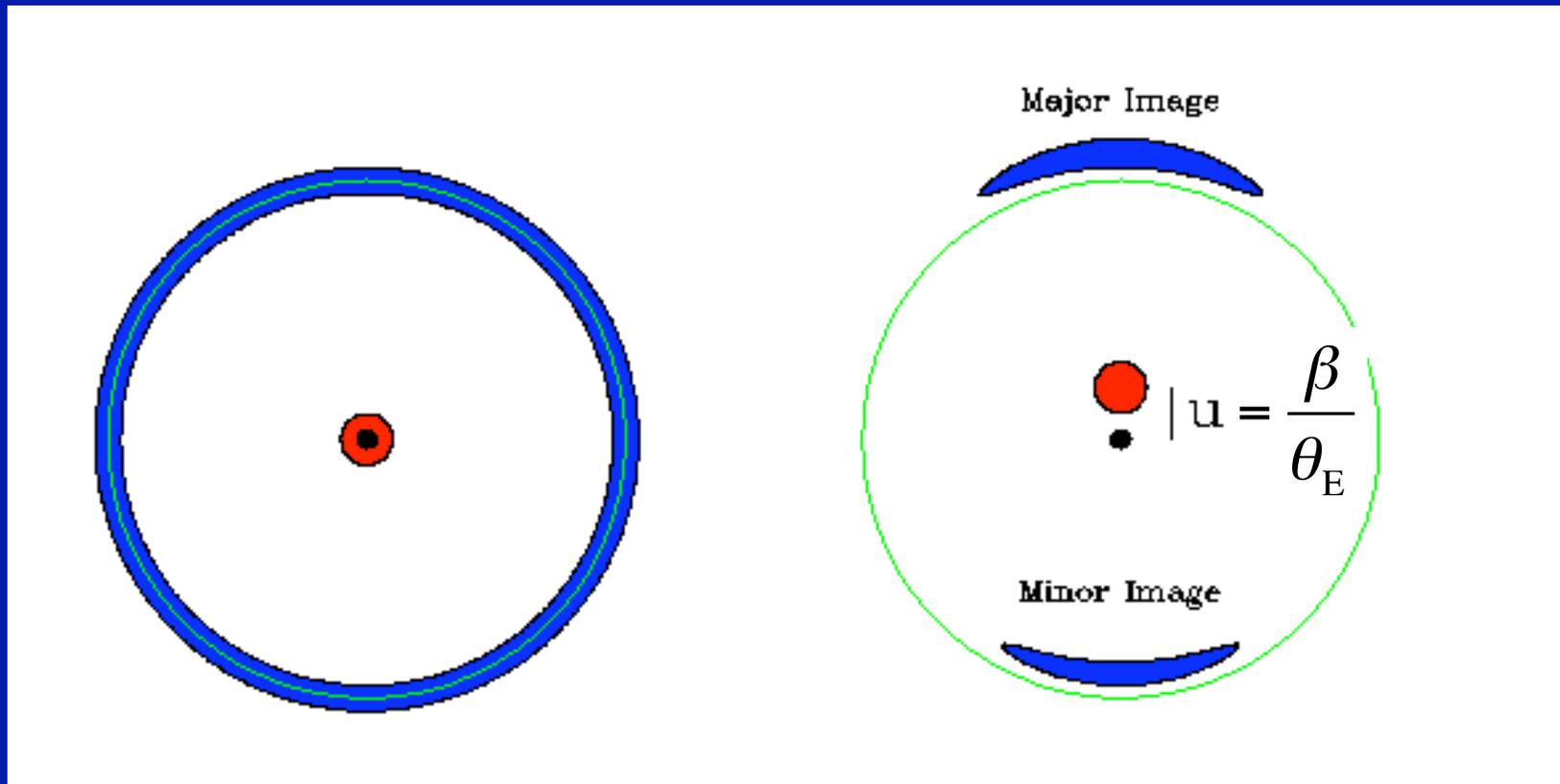
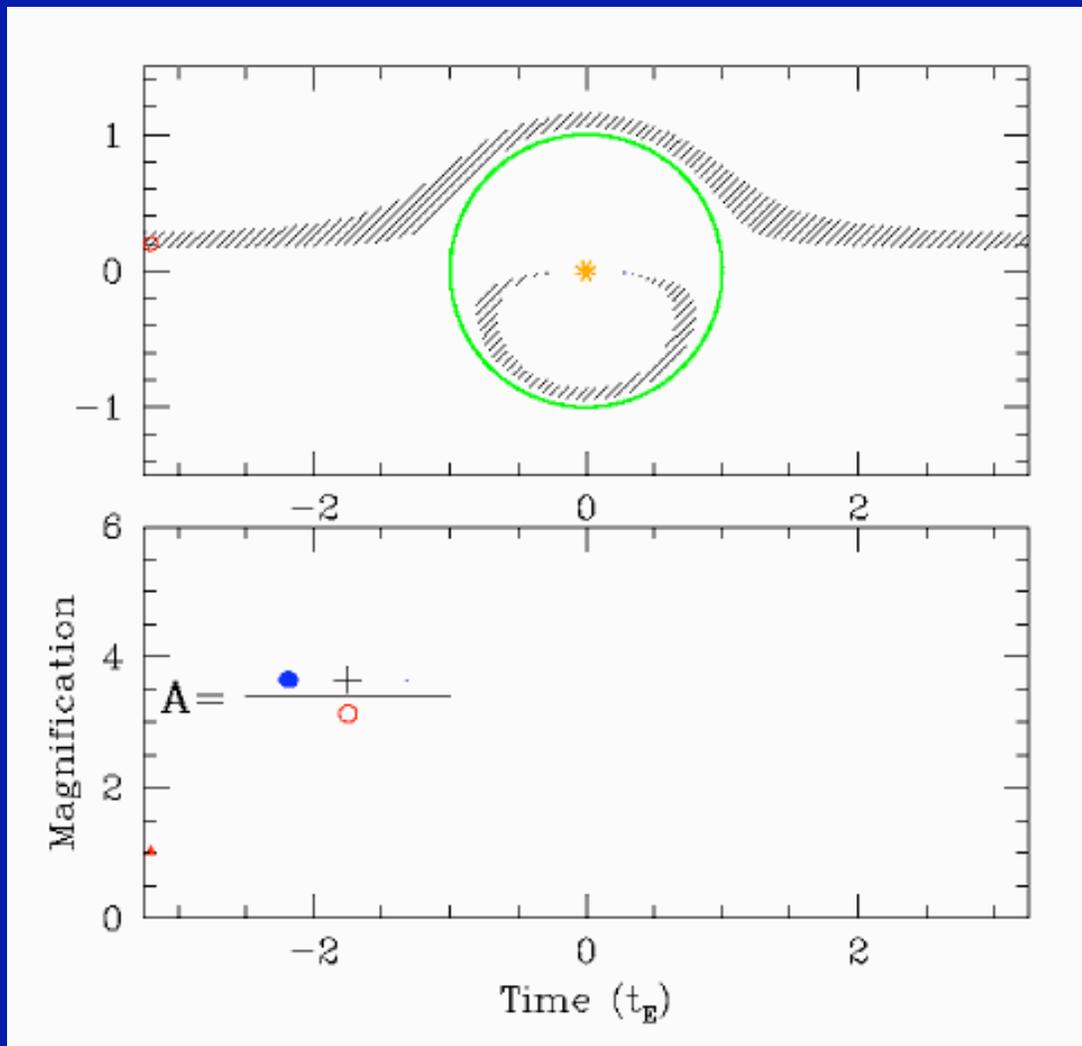


Image Separation  $\approx 2\theta_E$

Magnification  $= \frac{\text{Area of Image}}{\text{Area of Source}}$

# MICROLENSING EVENTS

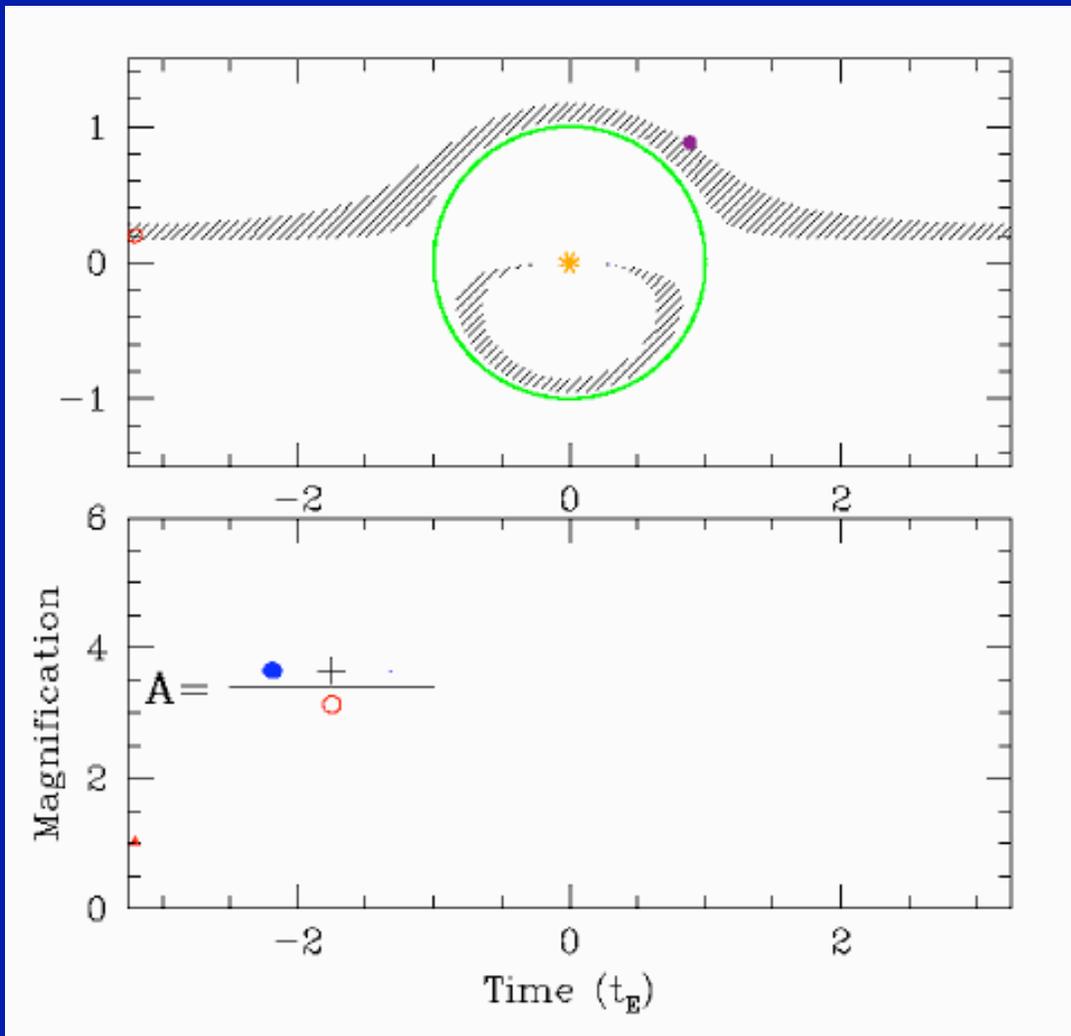


## Single Lens Parameters

- Impact Parameter
- Time of Maximum
- Timescale

$$t_E = \frac{\theta_E}{\mu} \approx 20 \text{ days} \left( \frac{M}{0.3M_\odot} \right)^{1/2}$$

# DETECTING PLANETS



## Single Lens Parameters

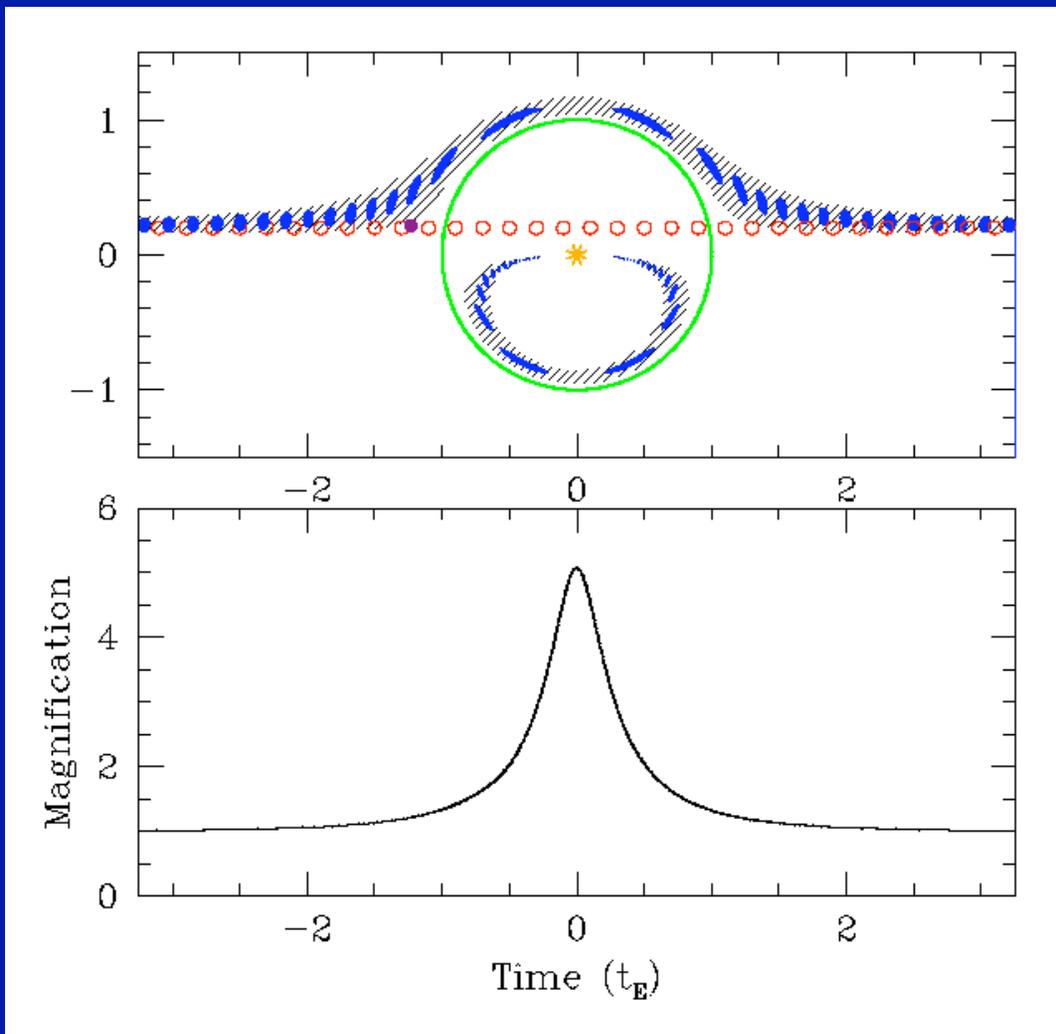
- Impact Parameter
- Time of Maximum
- Timescale

## Planet Parameters

- Angle wrt Binary Axis
- Projected Separation
- Mass Ratio

$$t_p = q^{1/2} t_E \approx 1 \text{ day} \left( \frac{M_p}{M_j} \right)^{1/2}$$

# DETECTION PROBABILITY



## Detection Probability

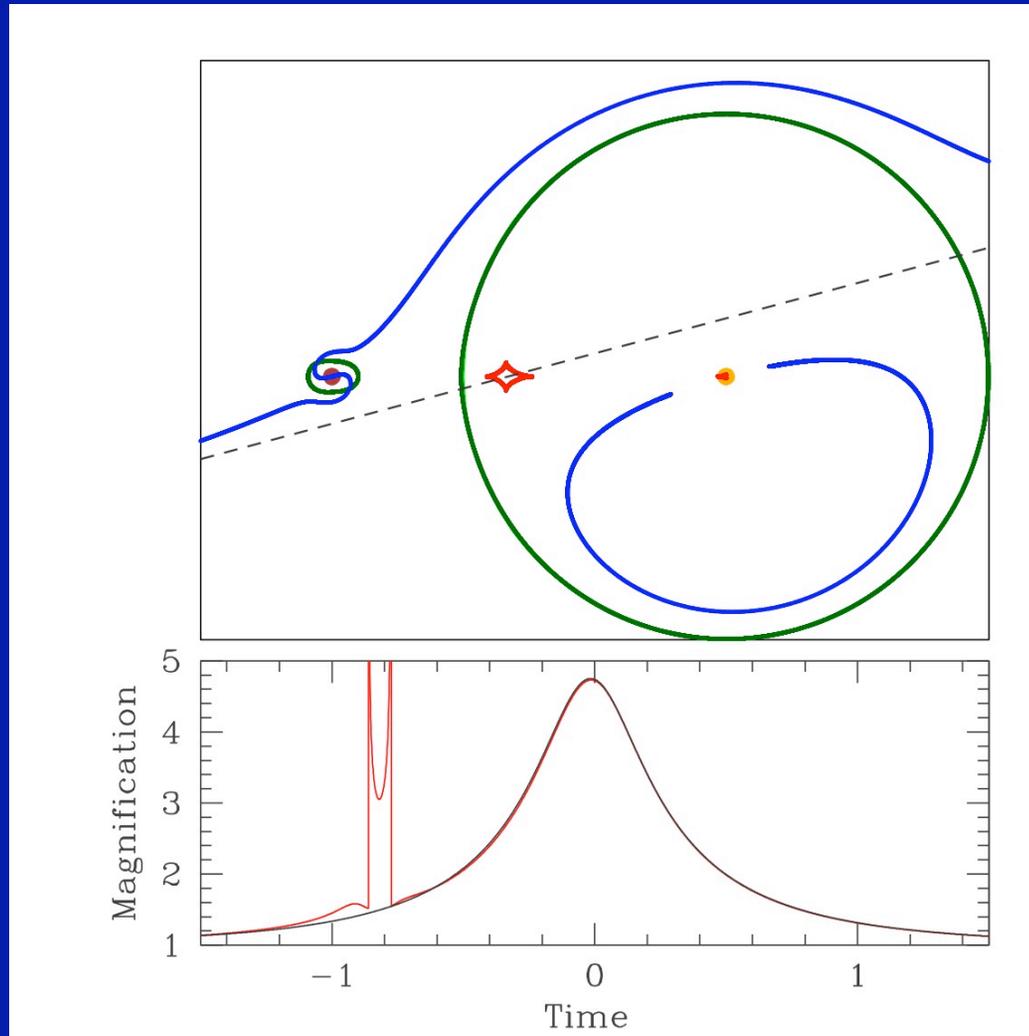
$$P \approx A \frac{\theta_p}{\theta_E} \approx 15\% \left( \frac{q}{10^{-3}} \right)^{1/2}$$

High-Magnification  $\rightarrow$   
High Efficiency

Maximized when

$$a \approx R_E = D_{OL} \theta_E \approx 3 \text{ AU}$$

# HIGH MAGNIFICATION EVENTS



**Why high-mag events rule:**

**Nearly 100% efficiency.**

(Griest & Safizadeh 1998)

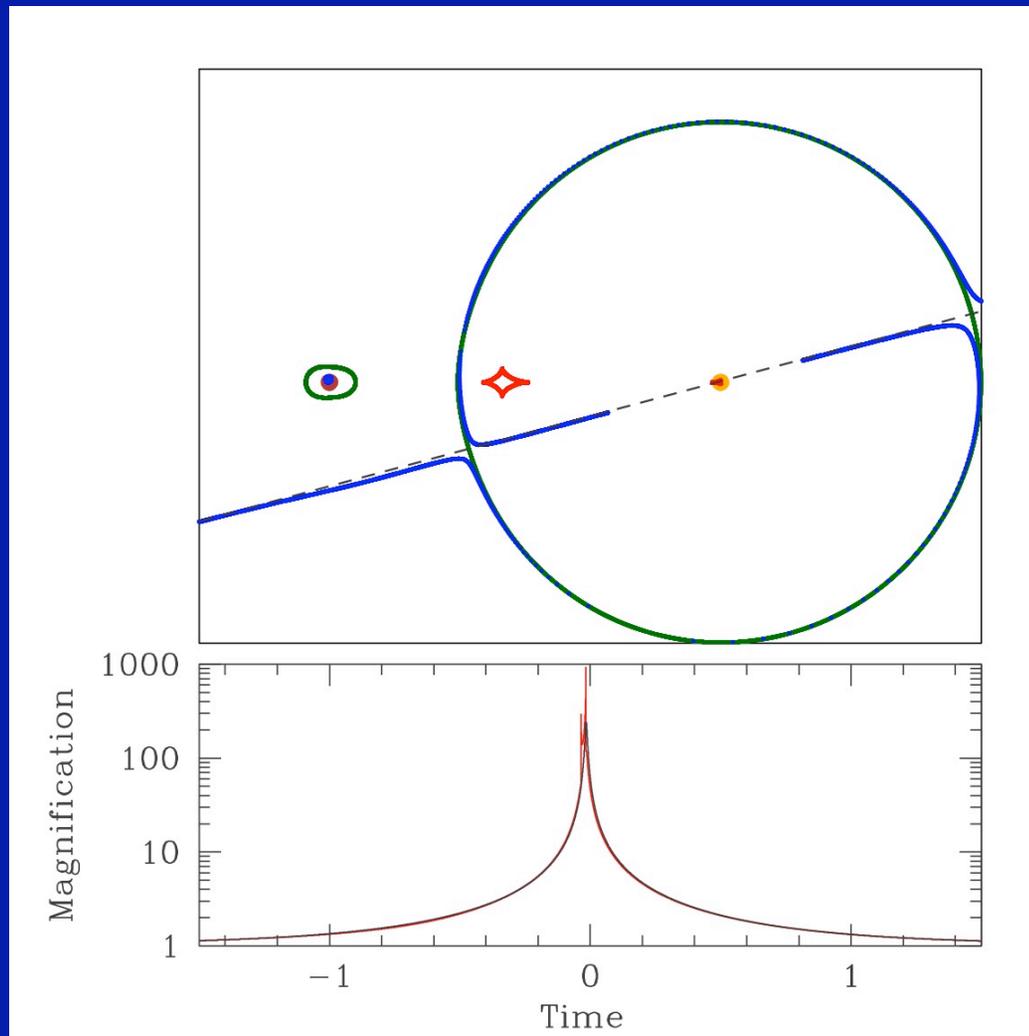
**Localized perturbations.**

**Predictable.**

**Multiple planets! (Gaudi et al. 1998)**

(planets in binaries including circumbinary planets)

# HIGH MAGNIFICATION EVENTS



**Why high-mag events rule:**

Nearly 100% efficiency.

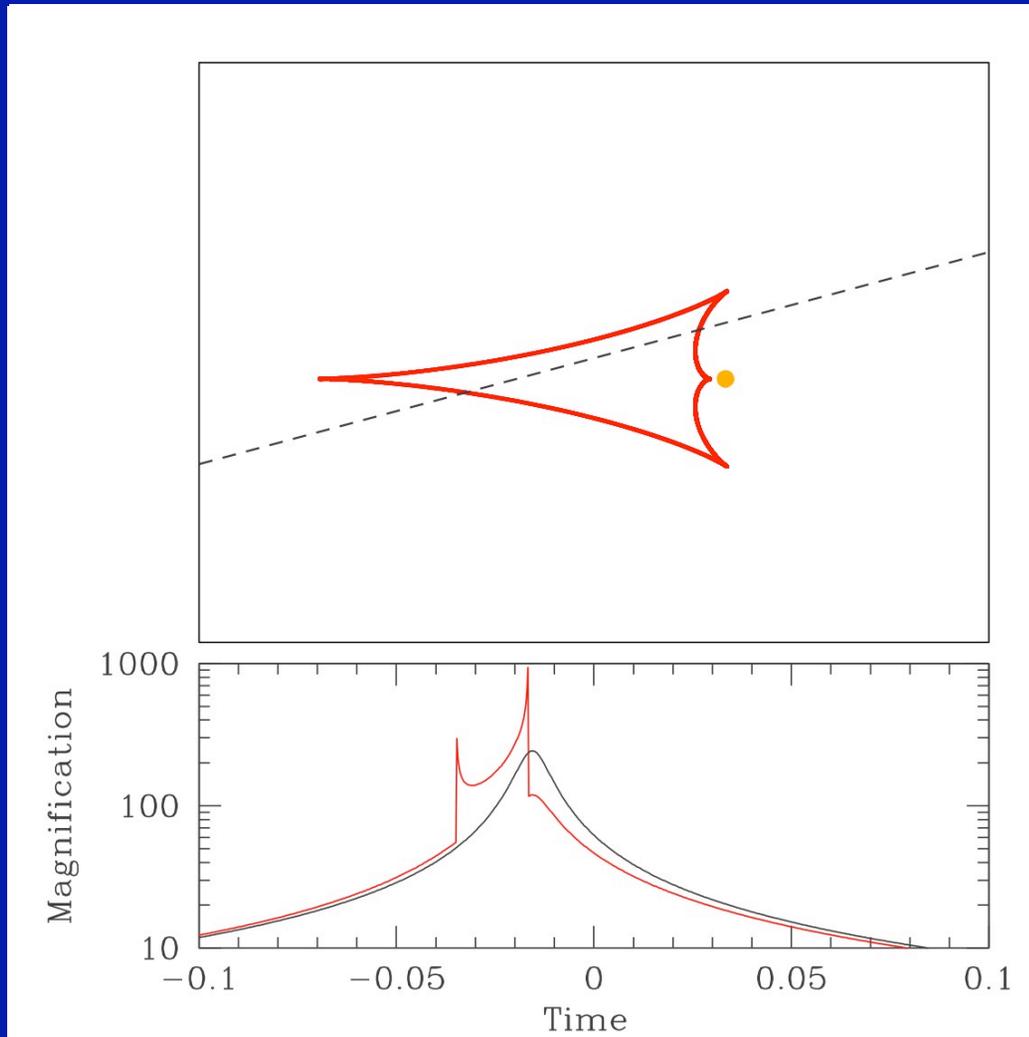
(Griest & Safizadeh 1998)

Localized perturbations.

Predictable.

**Multiple planets!** (Gaudi et al. 1998)  
(planets in binaries including  
circumbinary planets)

# HIGH MAGNIFICATION EVENTS



**Why high-mag events rule:**

Nearly 100% efficiency.

(Griest & Safizadeh 1998)

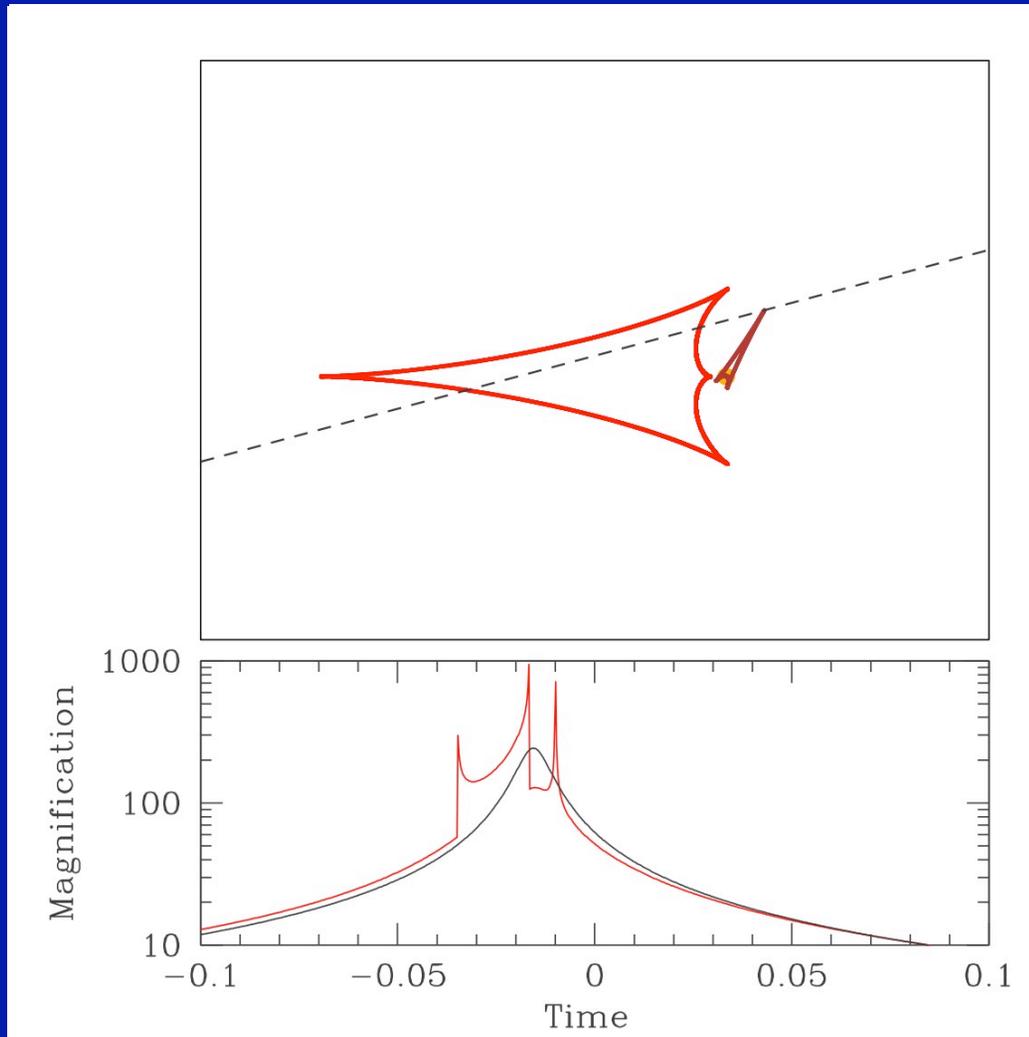
Localized perturbations.

Predictable.

**Multiple planets!** (Gaudi et al. 1998)

(planets in binaries including  
circumbinary planets)

# HIGH MAGNIFICATION EVENTS



**Why high-mag events rule:**

Nearly 100% efficiency.

(Griest & Safizadeh 1998)

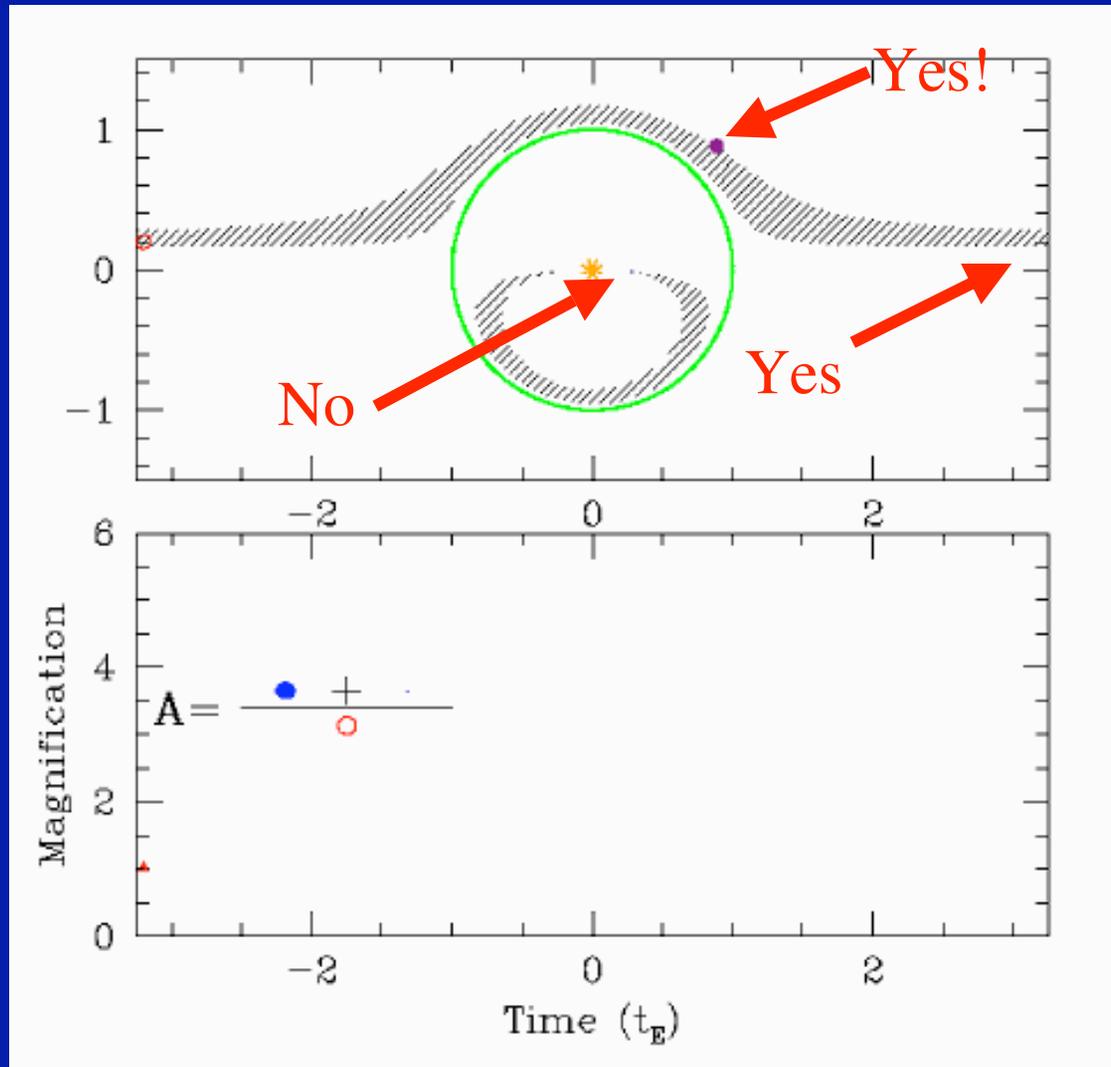
Localized perturbations.

Predictable.

**Multiple planets!** (Gaudi et al. 1998)

(planets in binaries including  
circumbinary planets)

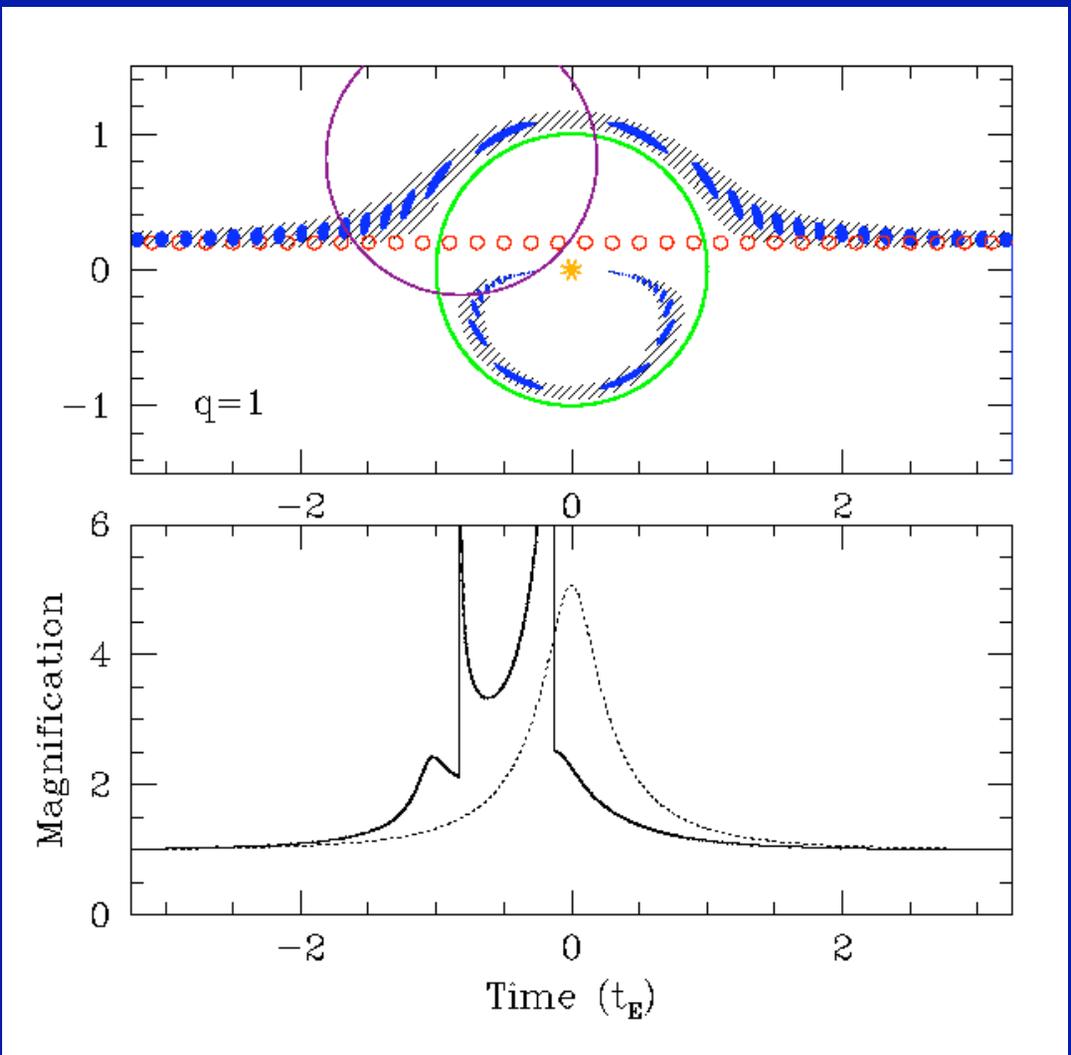
# MICROLENSING IS DIRECTLY SENSITIVE TO PLANET MASS



- Works by perturbing images
- Does not require light from the lens or planet.
- Sensitive to planets in the disk and bulge with  $D_{OL}=1-8$  kpc
- Sensitive to wide or free-floating planets
- Not sensitive to very close planets

# VERY LOW MASS PLANETS

Signal magnitude is *independent* of planet mass.



- Magnitude depends on separation of planet from image.
- Duration depends on mass.

$$t_p = q^{1/2} t_E \approx 2 \text{ hrs} \left( \frac{M_p}{M_{\oplus}} \right)^{1/2}$$

- Signals get rarer and briefer.
- Detection Probability  $\sim$  few %

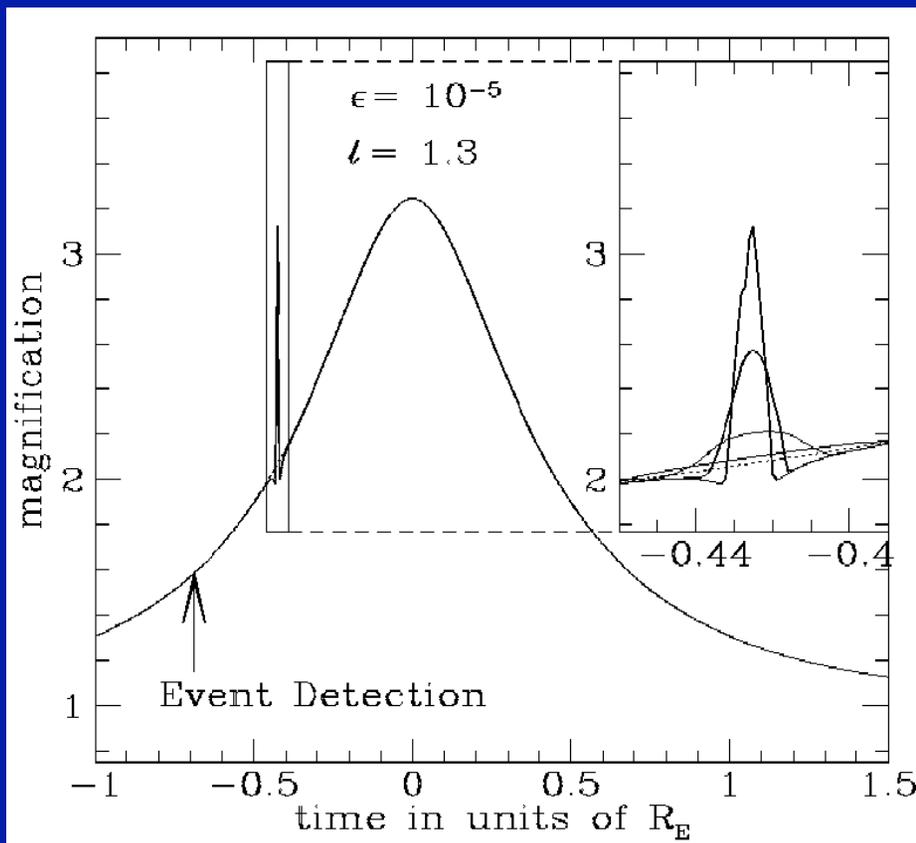
# HOW LOW CAN WE GO?

- Limited by Source Size

$$\rho_* = \frac{\theta_*}{\theta_E} \approx 1$$

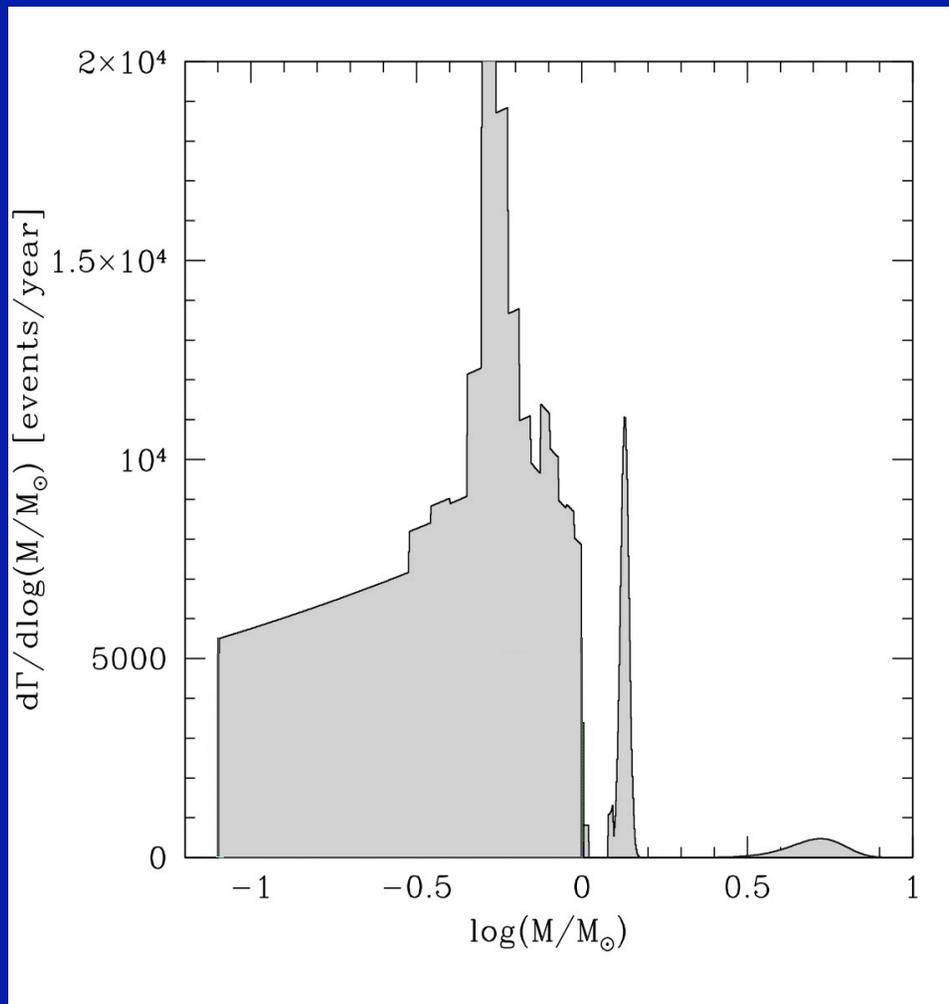
$$\theta_E \approx \mu \text{as} \left( \frac{M_p}{M_\oplus} \right)^{1/2} \longleftrightarrow \theta_* \approx \mu \text{as} \left( \frac{R_*}{R_\odot} \right)$$

**Mars-mass planets detectable  
if solar-type sources can be  
monitored!**



(Bennett & Rhie 1996)

# SENSITIVITY DEPENDS WEAKLY ON HOST MASS



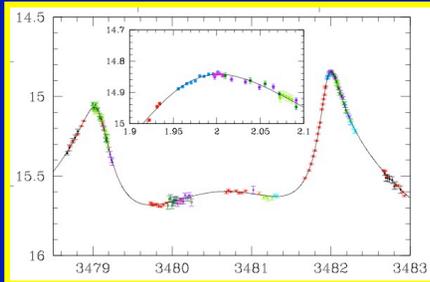
Sensitive to planets  
around:

- Main-sequence stars with  $M < M_{\odot}$
- Brown dwarfs
- Remnants

# FOUR

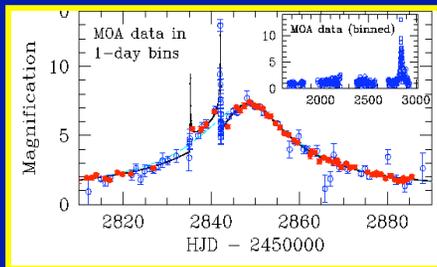
# DETECTIONS

OGLE-2005-BLG-071  
(Udalski et al 2005)



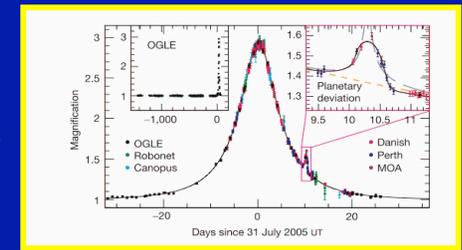
$M_p \sim 2.2M_J$ ,  $r \sim 3.7\text{AU}$

OGLE-2004-BLG-235  
MOA-2004-BLG-53  
(Bond et al 2004)



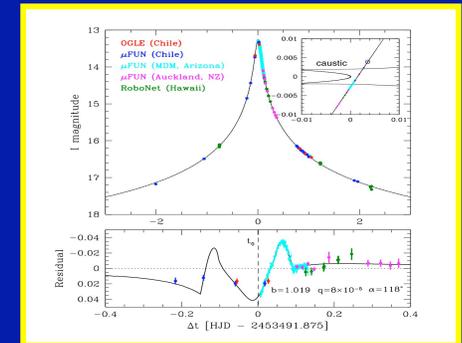
$M_p \approx 2.5M_J$ ,  $r \approx 4.3\text{AU}$

OGLE-2005-BLG-390  
(Beaulieu et al 2006)

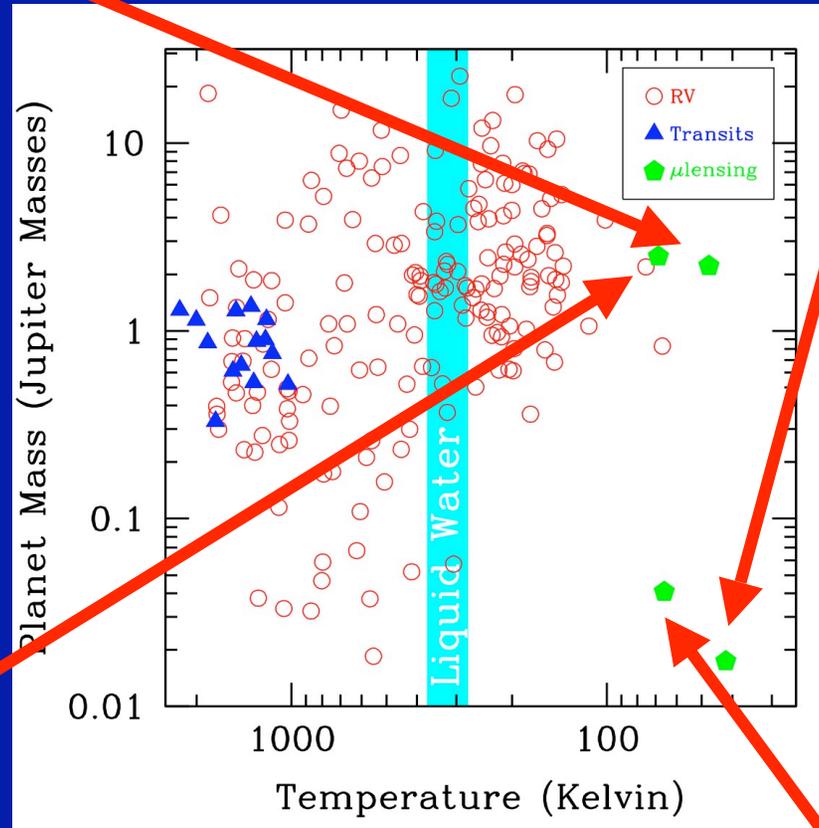


$M_p \sim 5.5M_{\oplus}$ ,  $r \sim 2.6\text{AU}$

OGLE-2005-BLG-169  
(Gould et al 2006)



$M_p \sim 13M_{\oplus}$ ,  $r \sim 3.5\text{AU}$



Two Jovian-mass planets  
Two Neptune-mass planets

# COOL NEPTUNES ARE COMMON

Two high-mass detections imply:

**Jupiter-mass planets are uncommon but not rare.**

Two low-mass detections imply:

**~37% of stars have Neptunes between 1.6-4.3 AU**

Also:

**Cool Neptunes are more common than cool Jupiters**

## A CONFESSION:

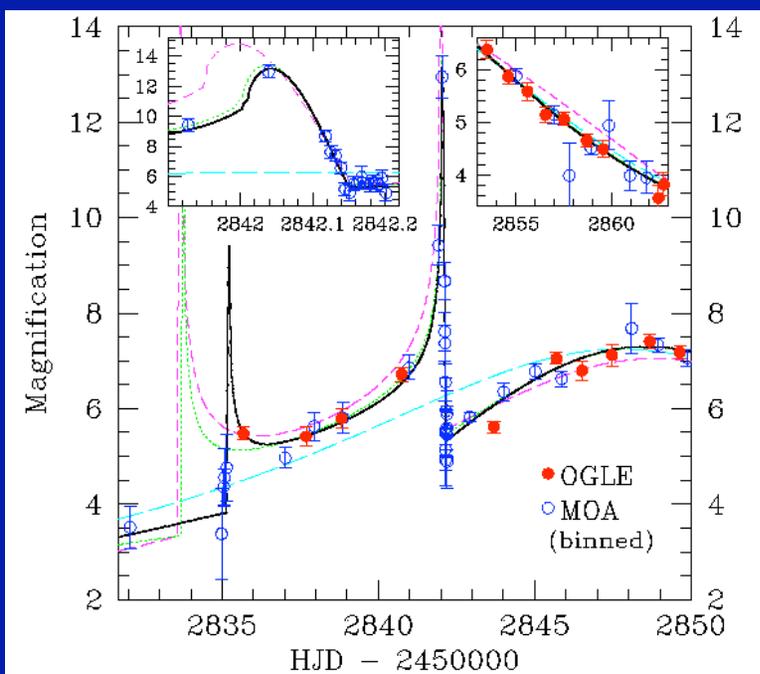
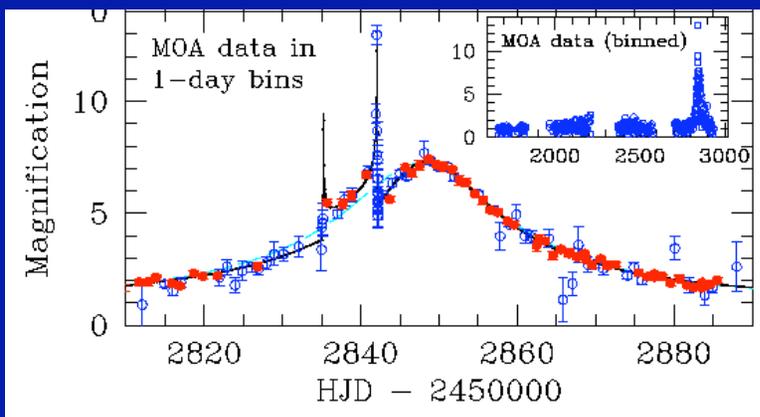
We've been lying to you.

Lie #1: Only measure mass ratio  
and timescale.

Lie #2: No information about host.

# CONSTRAINTS ON HOST

(Bond et al 2004, Bennett et al 2006)



Information from lightcurves:

- Measure  $q$ ,  $b$ ,  $t_E$  from lightcurve
- Detect influence of the source size
- Can determine  $\rho_*$  and so  $\theta_E$

$$\rho_* = \frac{\theta_*}{\theta_E}$$

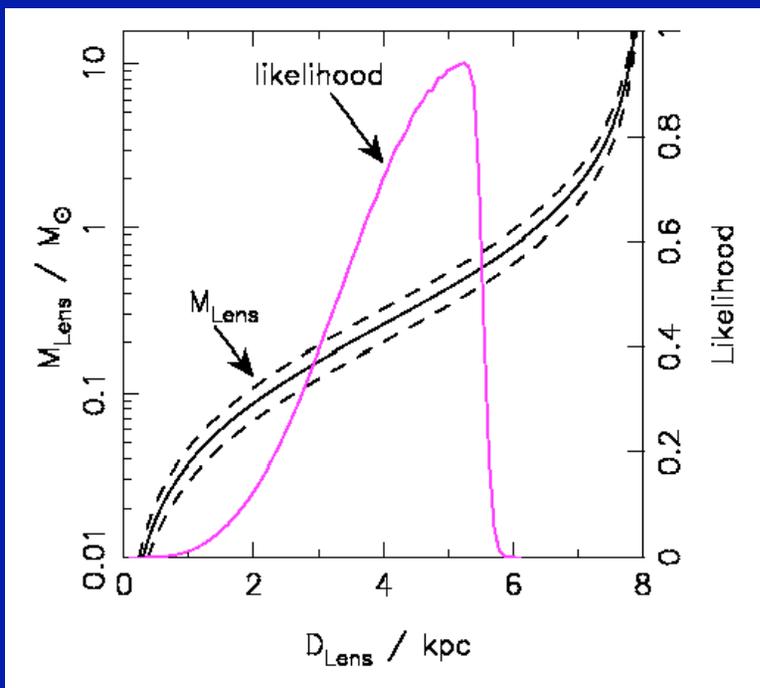
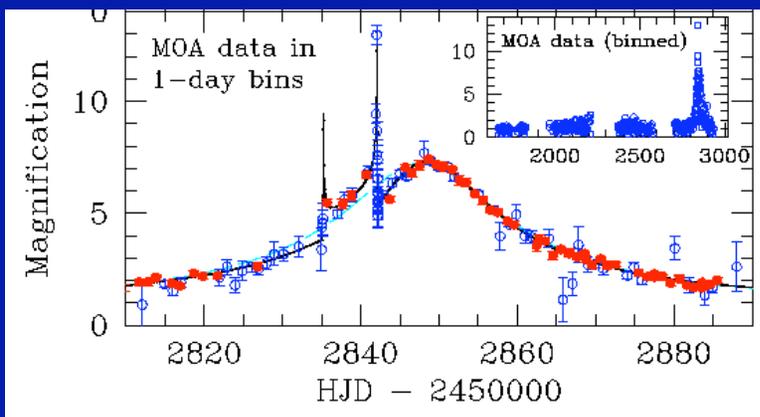


$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_{OL}D_{OS}}}$$

- Lens light yields lens mass
- Lens light can be detected by:
  - Resolving unrelated blended light
  - Waiting until lens and source separate
  - Measuring PSF elongation or centroid shift
- Measurement of host star mass

# CONSTRAINTS ON HOST

(Bond et al 2004, Bennett et al 2006)



Information from lightcurves:

- Measure  $q$ ,  $b$ ,  $t_E$  from lightcurve
- Detect influence of the source size
- Can determine  $\rho_*$  and so  $\theta_E$

$$\rho_* = \frac{\theta_*}{\theta_E}$$

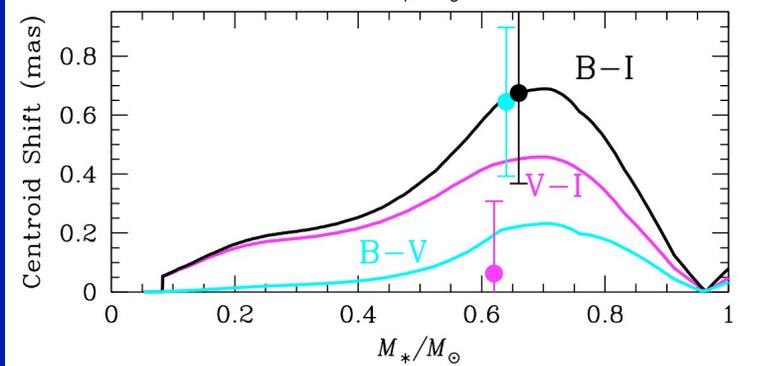
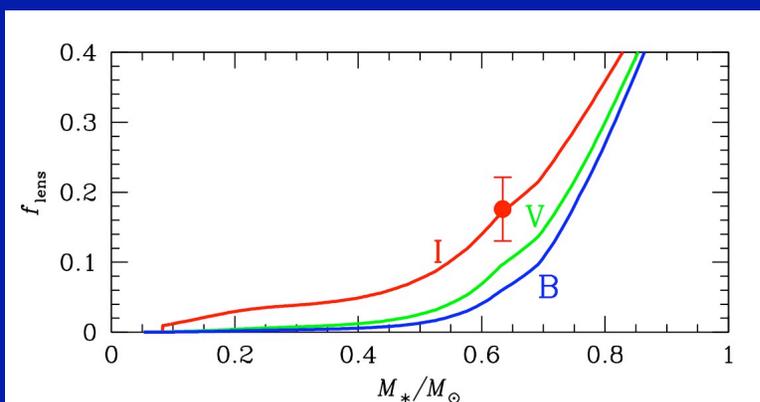
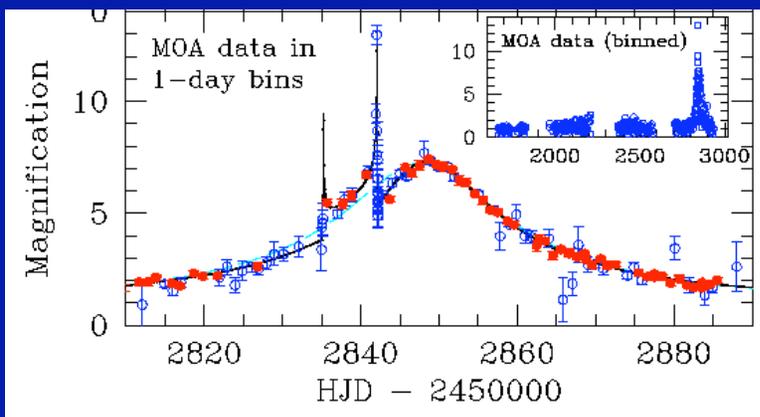


$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_{OL}D_{OS}}}$$

- Lens light yields lens mass
- Lens light can be detected by:
  - Resolving unrelated blended light
  - Waiting until lens and source separate
  - Measuring PSF elongation or centroid shift
- Measurement of host star mass

# CONSTRAINTS ON HOST

(Bond et al 2004, Bennett et al 2006)



Information from lightcurves:

- Measure  $q$ ,  $b$ ,  $t_E$  from lightcurve
- Detect influence of the source size
- Can determine  $\rho_*$  and so  $\theta_E$

$$\rho_* = \frac{\theta_*}{\theta_E}$$

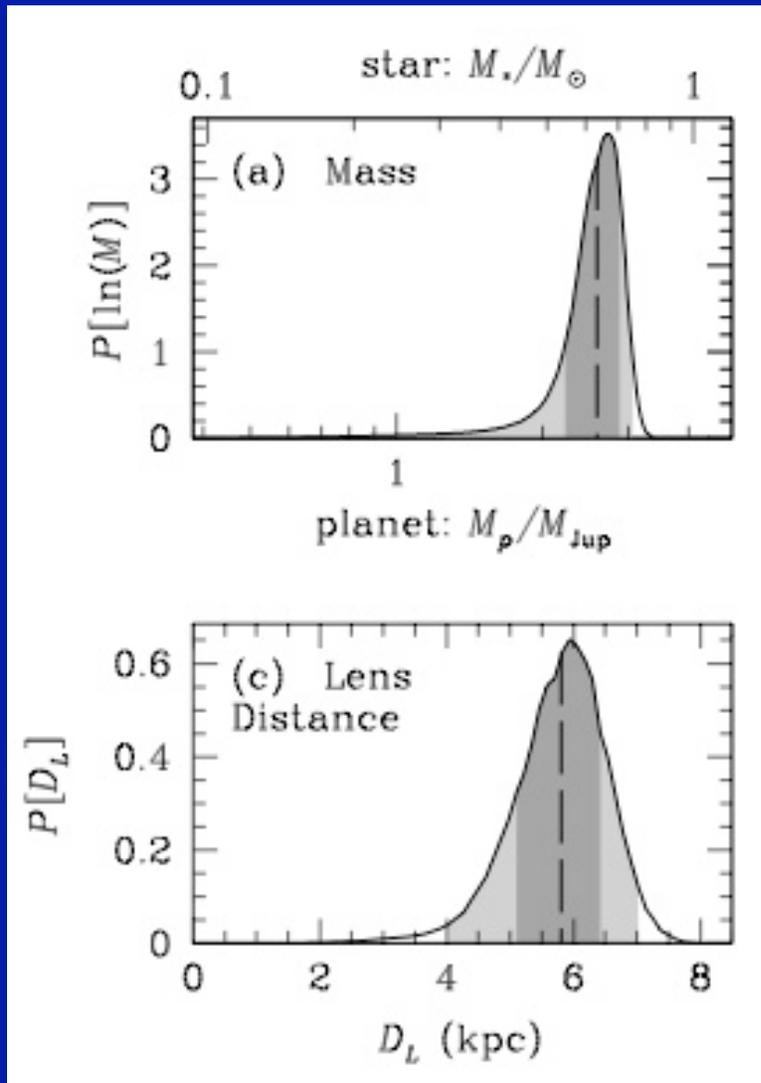


$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_{OL}D_{OS}}}$$

- Lens light yields lens mass
- Lens light can be detected by:
  - Resolving unrelated blended light
  - Waiting until lens and source separate
  - Measuring PSF elongation or centroid shift
- Measurement of host star mass

# CONSTRAINTS ON HOST

(Bond et al 2004, Bennett et al 2006)



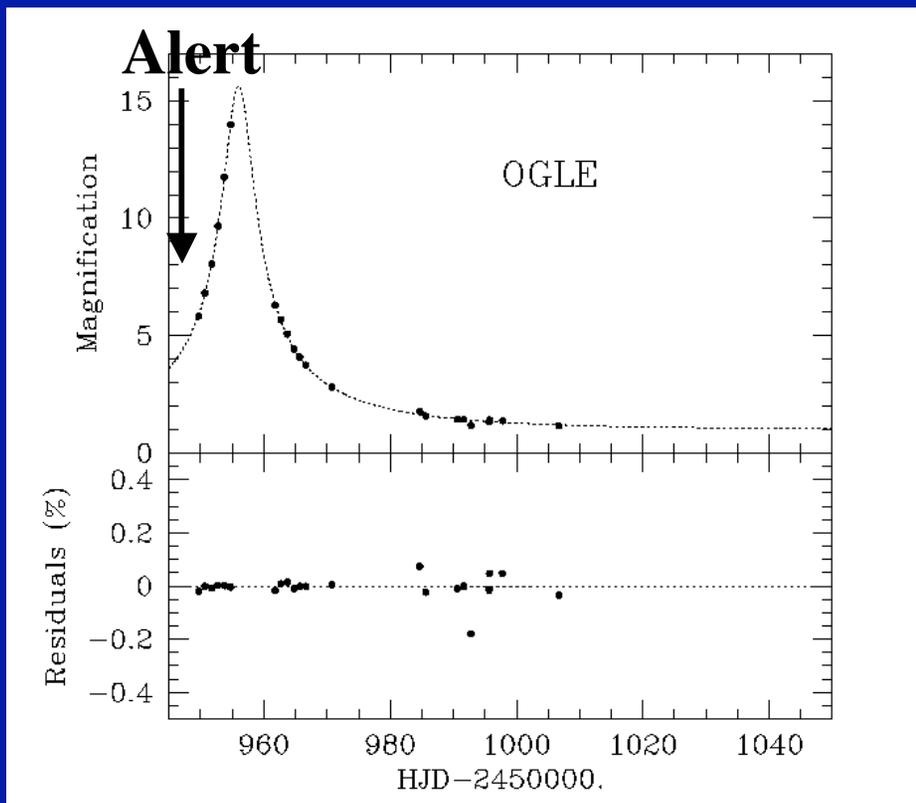
Information from lightcurves:

- Measure  $q$ ,  $b$ ,  $t_E$  from lightcurve
- Detect influence of the source size
- Can determine  $\rho_*$  and so  $\theta_E$

$$\rho_* = \frac{\theta_*}{\theta_E} \rightarrow \theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_{OL}D_{OS}}}$$

- Lens light yields lens mass
- Lens light can be detected by:
  - Resolving unrelated blended light
  - Waiting until lens and source separate
  - Measuring PSF elongation or centroid shift
- Measurement of host star mass

# HOW IT IS DONE : ALERTS



## “Survey Collaborations”

- Monitor the bulge
- Insufficient sampling
- Real-time Alerts

MACHO, EROS, OGLE, MOA

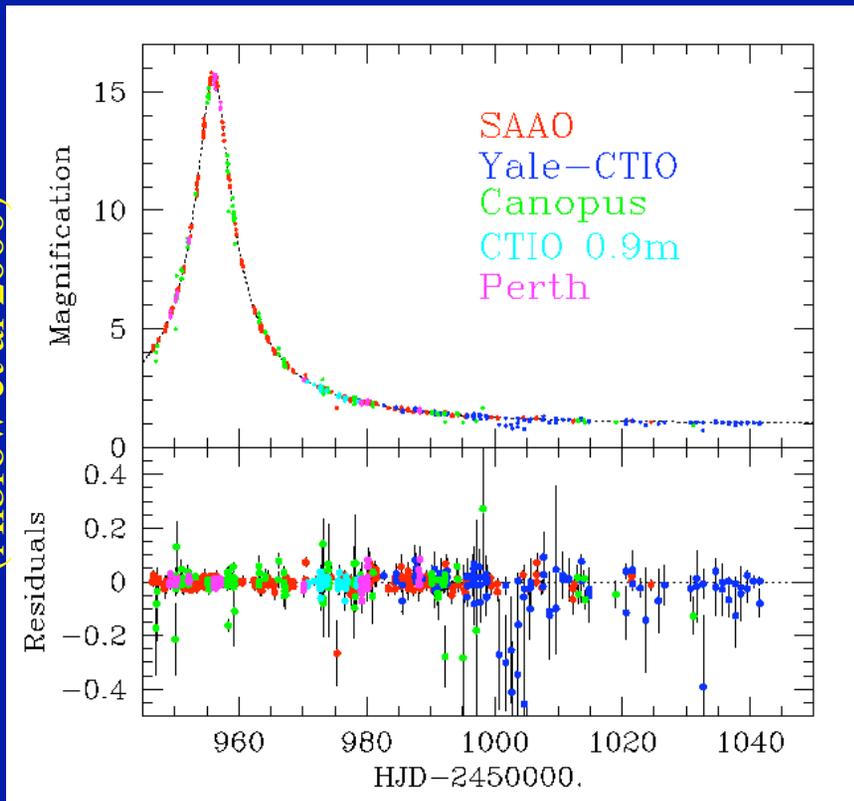
## “Follow-Up Collaborations”

- Monitor microlensing events
- High cadence and optimized photometry

GMAN, MPS, EXPORT, PLANET,  $\mu$ FUN

# HOW IT IS DONE : FOLLOW-UP

(Albrow et al 2000)



Median Sampling  $\sim$  1 hour  
RMS scatter over peak  $\sim$  1.5%

## “Survey Collaborations”

- Monitor the bulge
- Insufficient sampling
- Real-time Alerts

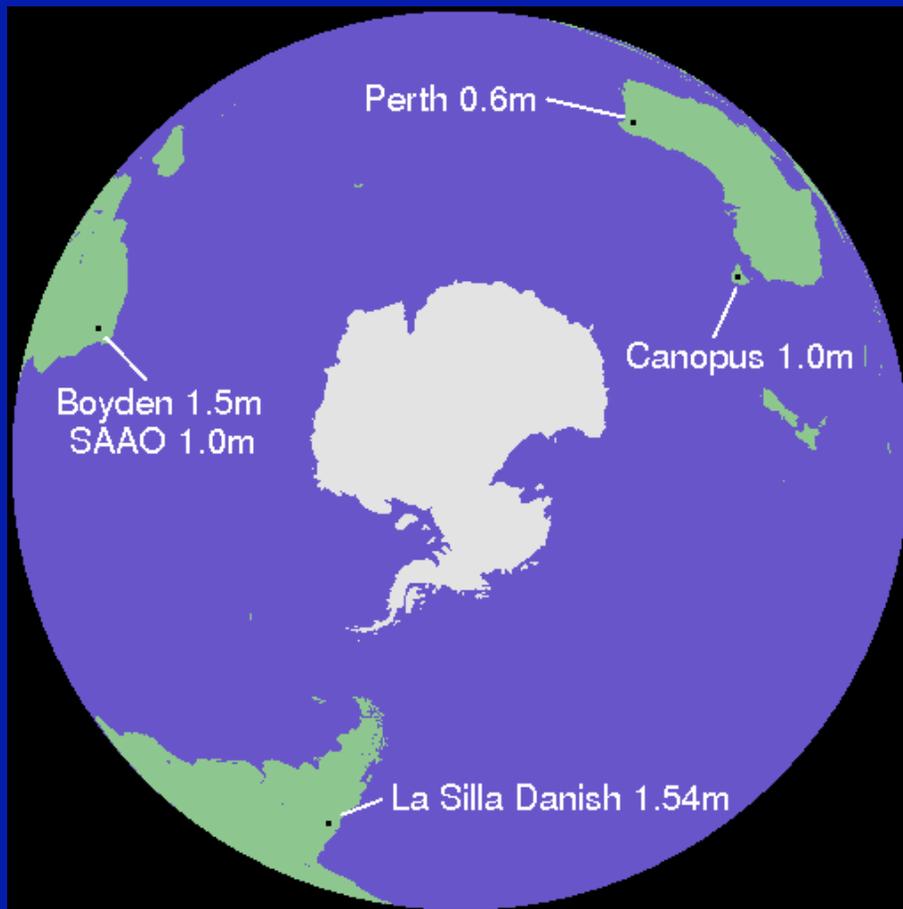
MACHO, EROS, OGLE, MOA

## “Follow-Up Collaborations”

- Monitor microlensing events
- High cadence and optimized photometry

GMAN, MPS, EXPORT, PLANET,  $\mu$ FUN

# PLANET: FOLLOW EVERYTHING YOU CAN



## Distributed network:

- Cover as many events as possible
- Dense coverage of many events

## Led to detection of the lowest mass exoplanet

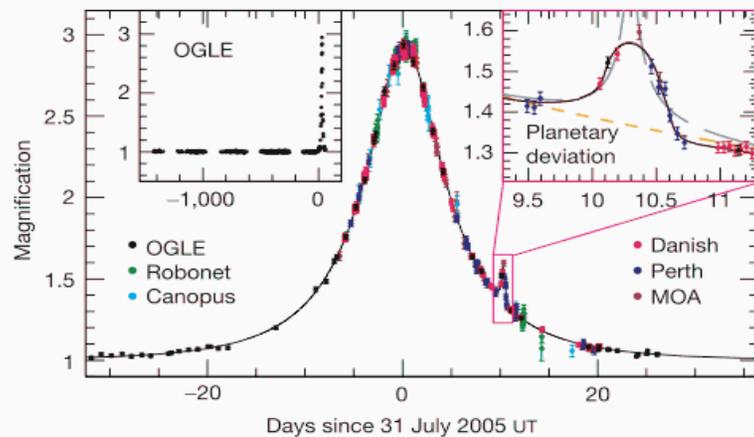
- Individual probability very low
- Only possible because of the PLANET approach
- Took 10 years!

# PLANET: FOLLOW EVERYTHING YOU CAN

OGLE-2005-BLG-390  
(Beaulieu et al 2006)

Distributed network:

- Cover as many events as possible
- Dense coverage of many events



Led to detection of the lowest mass exoplanet

- Individual probability very low
- Only possible because of the PLANET approach
- Took 10 years!

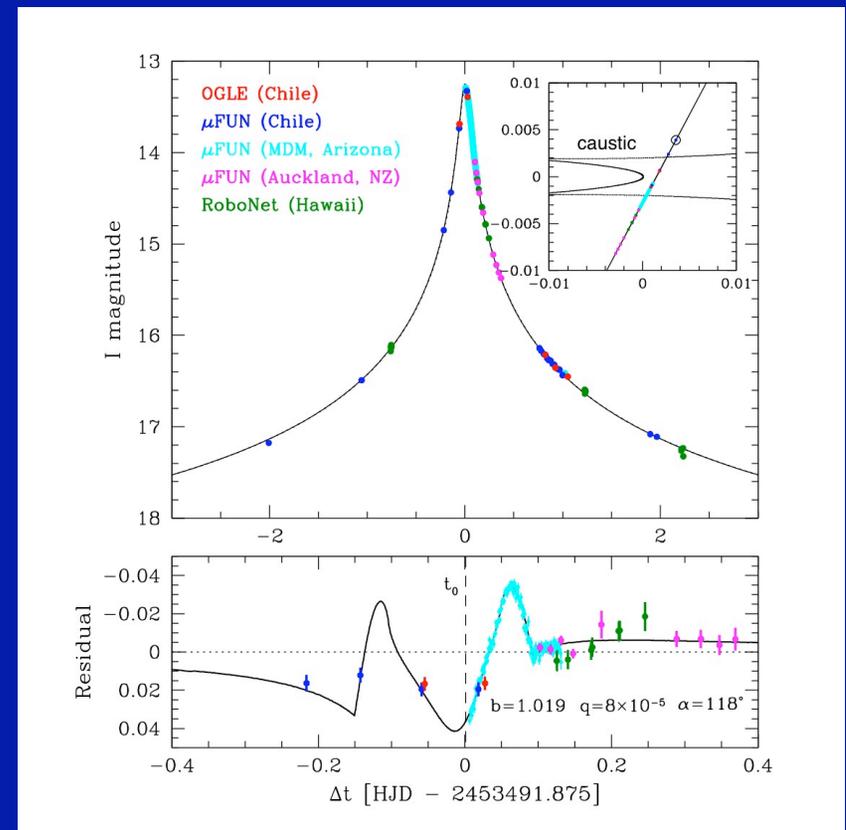
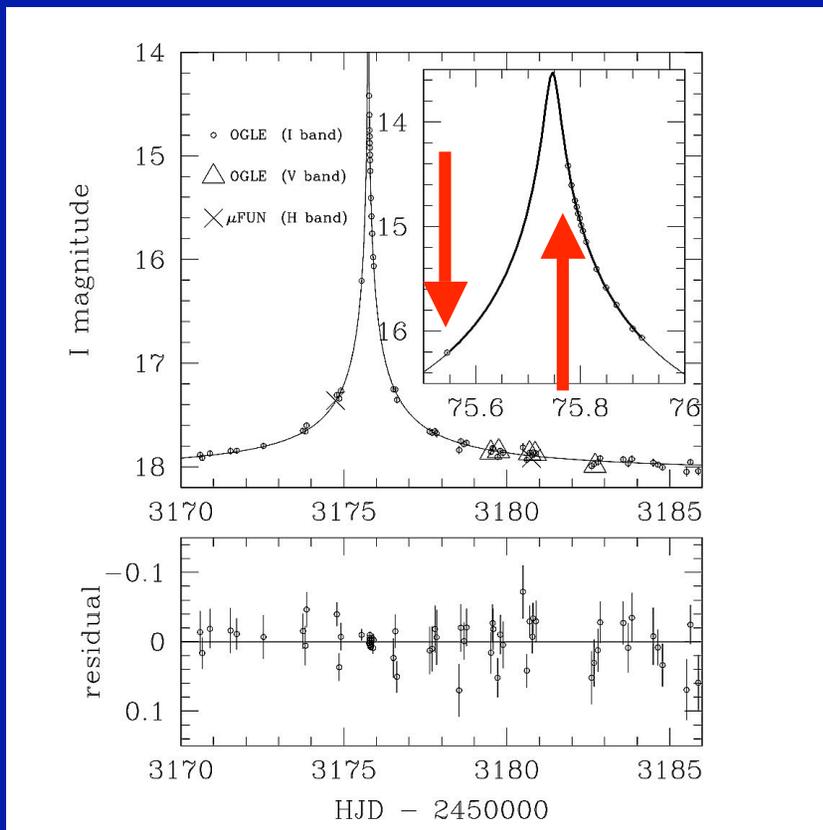
$$M_p \sim 5.5 M_{\oplus}, \quad r \sim 2.6 \text{ AU}$$

# CURRENT SHOE-STRING, SLIPSHOD $\mu$ FUN APPROACH

- Focus on high-magnification events
- Struggle to identify events real time
- Save money by employing enthusiastic amateurs
- Wait.... wait... wait.... PANIC!

# THE ELUSIVE HIGH-MAGNIFICATION EVENT

The one that got away... ...and the one that didn't

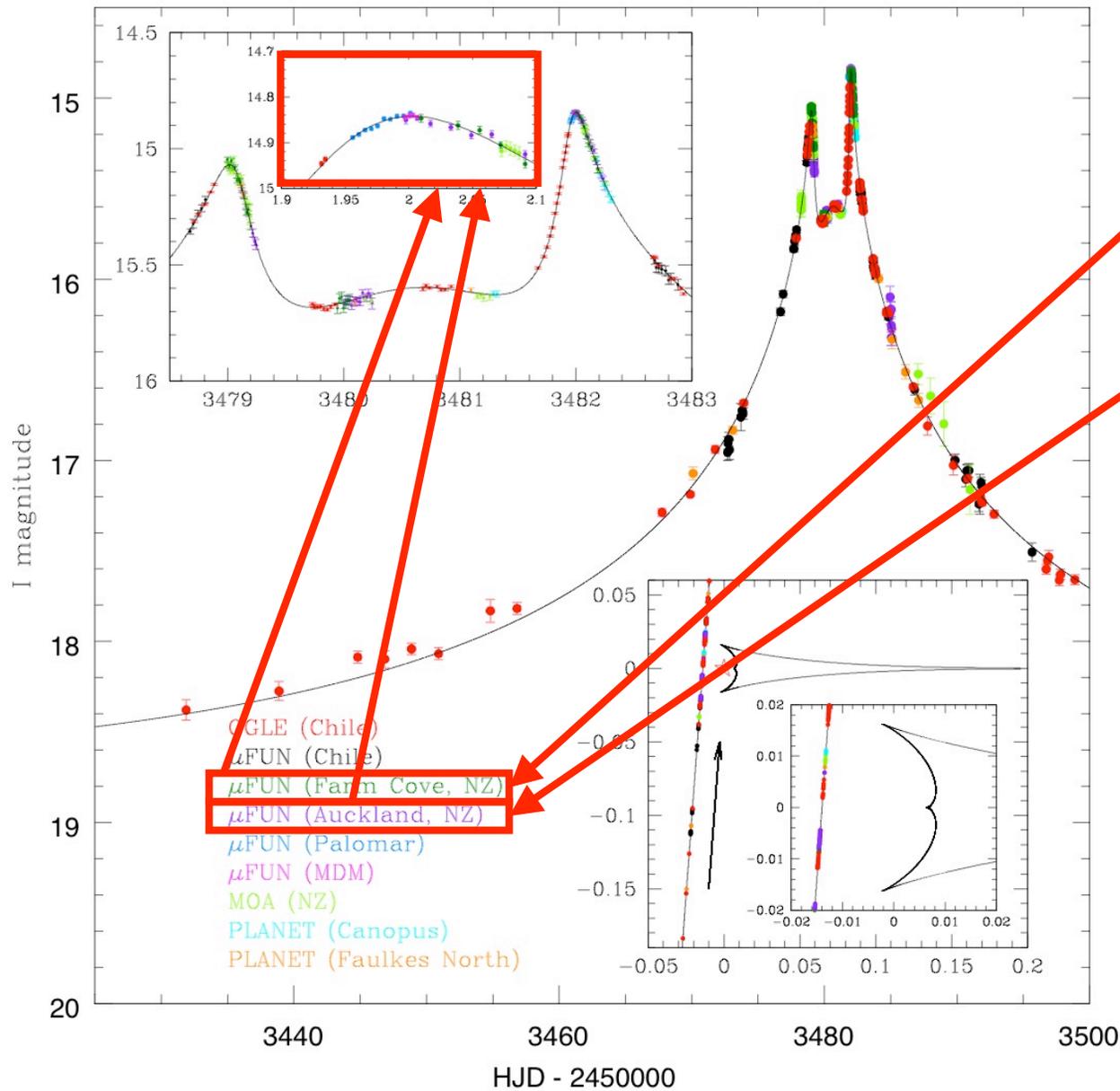


(would have had sensitivity to Earth-mass planets)

# AMAZING AMATEURS

- Auckland Observatory (0.4-meter)
- Bronberg Observatory (0.4-meter )
- Catino Austral Observatory (0.4-meter)
- **CTIO** (1.3-meter)
- Farm Cove Observatory (0.4-meter)
- Hunters Hill Observatory (0.4-meter)
- **MDM Observatory**, (2.4-meter)
- **Mt Lemmon Observatory** (1.0-meter)
- **Palomar Observatory** (60-inch)
- Perth (0.3-meter)
- Southern Stars Observatory (0.3-meter)
- Vintage Lane Observatory (0.4-meter)
- **Wise Observatory** (1.0-meter)





**0.35m!!**

**0.4m!!**

*“It just shows that you can be a mother, you can work full-time, and you can still go out there and find planets.”*

*-Jenny McCormick*

*Farm Cove Observatory*

# WHAT'S NEXT?

- **Current setup (alert/follow-up) saturated**
  - Nearly all of the useable bulge monitored
  - Many events cannot be monitored
  - Monitoring one event at a time too inefficient
- **A new strategy**
  - Dispense with alert/follow-up
  - Simultaneously detect and monitor microlensing events

# WHAT IS REQUIRED?

## Detecting the Perturbations from Earth-mass Planets

- Sampling rate  $\sim$  10 minutes

$$t_{E,p} = 2\text{hrs} \left( \frac{M_p}{M_E} \right)^{1/2}$$

- Photometric Accuracy  $\sim$  1% at  $I \sim 21$

– Signal Magnitude

$$\frac{\Delta F}{F} \approx 1\% \left( \frac{M_p}{M_\oplus} \right) \left( \frac{R_*}{R_\odot} \right)^{-2}$$

– Photometric Uncertainty

$$\sigma = 1\% \left( \frac{D}{2\text{m}} \right)^{-1} \left( \frac{t_{\text{exp}}}{120\text{s}} \right)^{-1/2} 10^{0.2(I-21)}$$

# WHAT IS REQUIRED?

- Event Rate

- Primary Event Rate

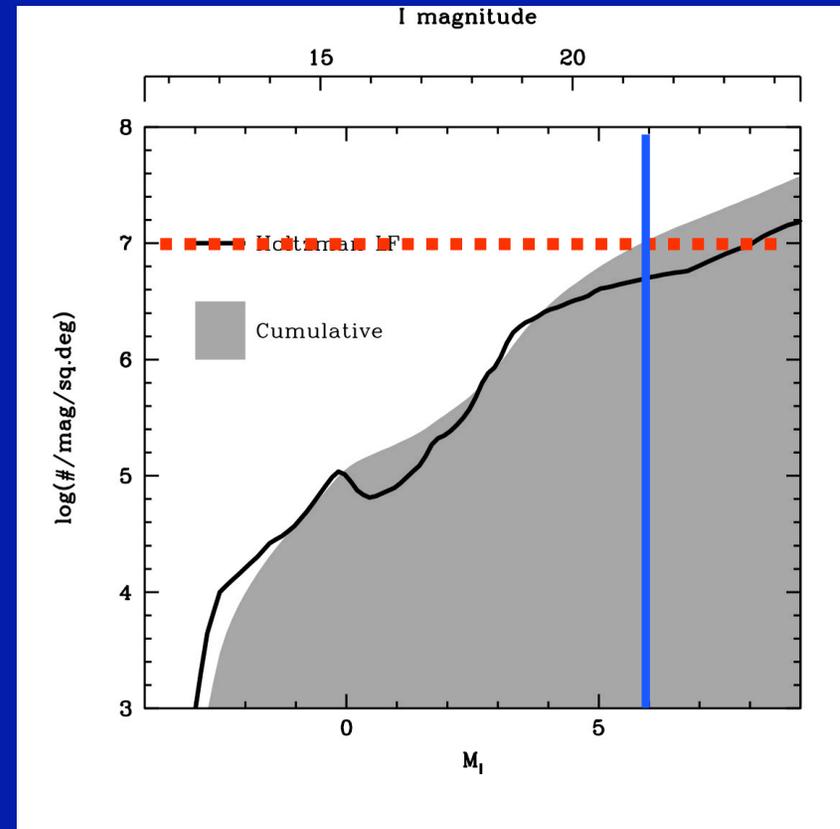
$$\Gamma \approx 10^{-5} \text{ yr}^{-1}$$

- Detection Probability

$$P \approx A_0 \theta_p \approx 1\% \left( \frac{M_p}{M_{\text{Earth}}} \right)^{1/2}$$

- Detections Per Year

$$N \approx n_F \Omega \Phi \Gamma P \approx 10 \text{ yr}^{-1} \left( \frac{\Omega}{10 \square^\circ} \right) \left( \frac{\Phi}{10^7 / \square^\circ} \right) \left( \frac{\Gamma}{10^{-5} \text{ yr}^{-1}} \right) \left( \frac{P}{1\%} \right)$$



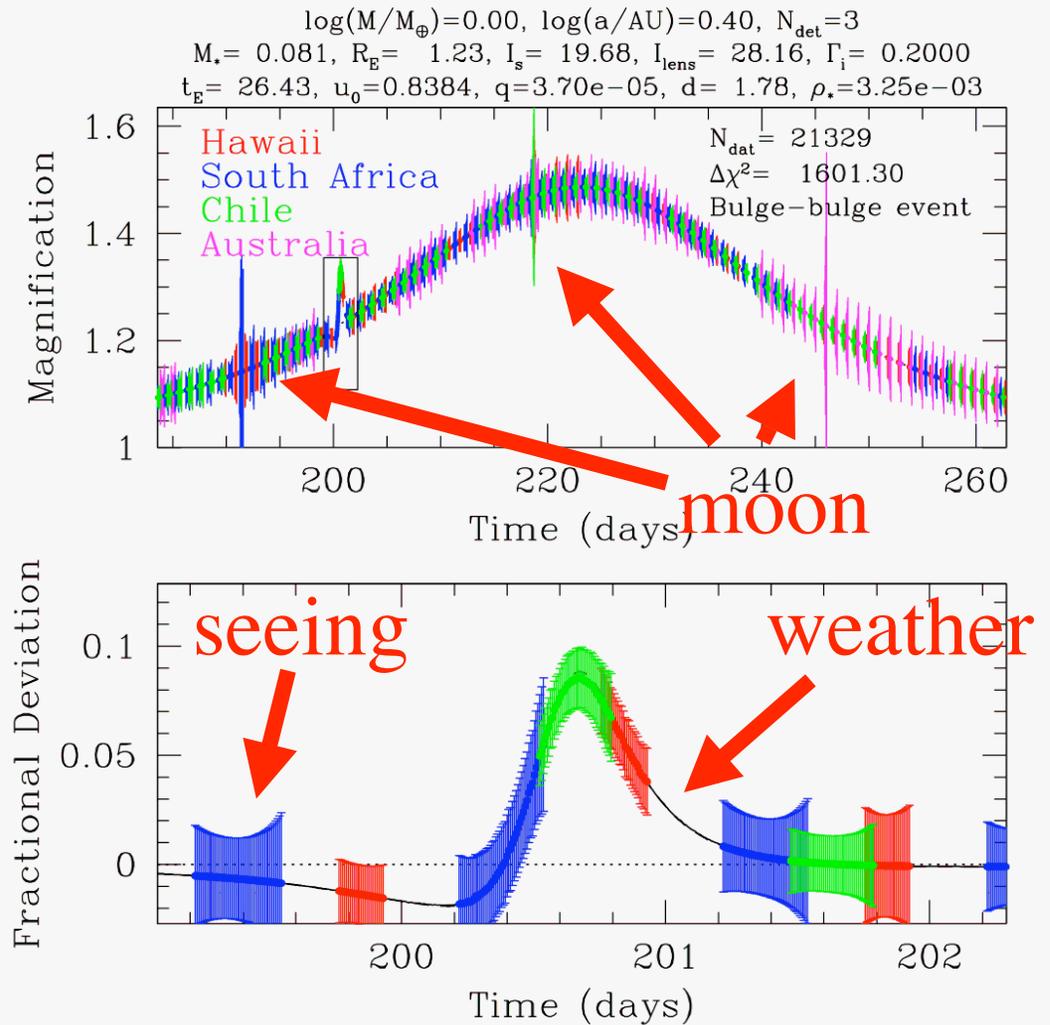
# NEXTGEN $\mu$ LENSING SURVEY

- Requirements to detect  $\sim 10$  Earth-mass planets per year
  - Monitor  $\sim 10$  square degrees of the Galactic bulge continuously with  $\sim 10$  minute sampling using 1-2m class telescopes
- Monte Carlo simulation
  - Survey specifications
    - Four 2m telescopes in Hawaii, Chile, South Africa and Australia
    - 4 square degree cameras
    - 4 fields in the bulge (16 square degrees, 7000 events per year)

# SIMULATION INGREDIENTS

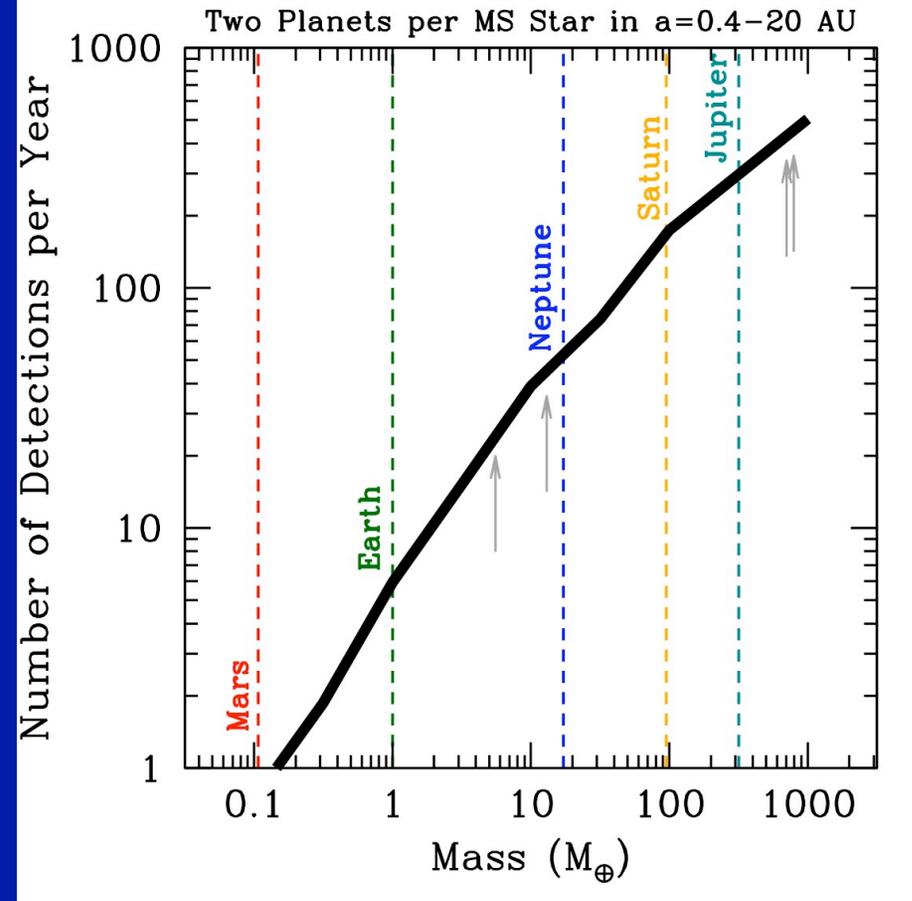
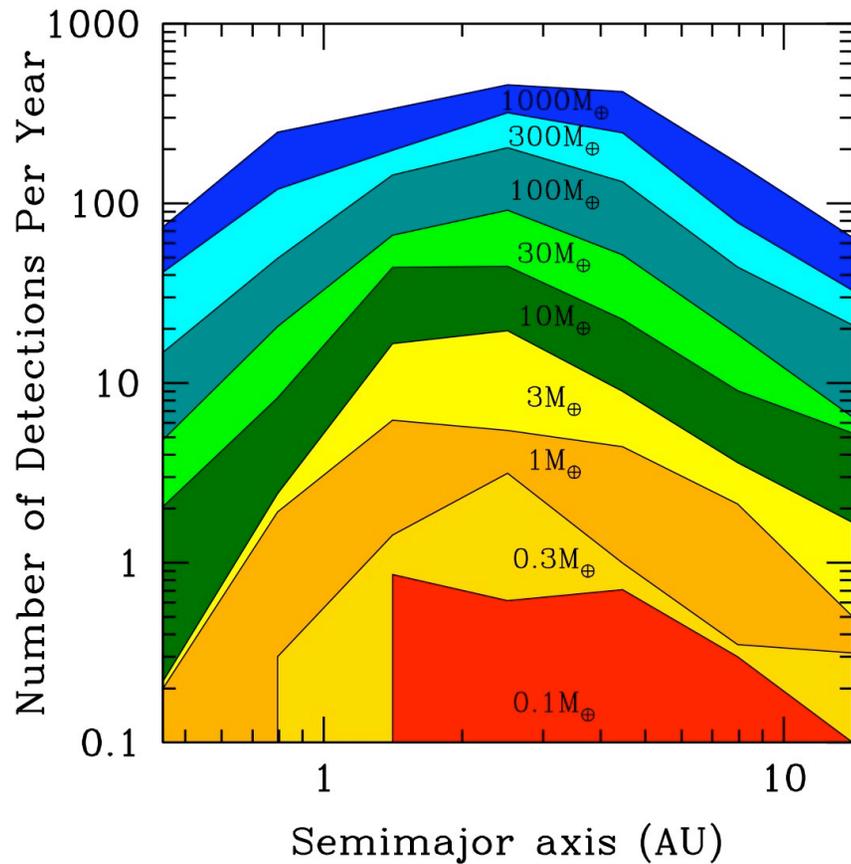
## Monte Carlo Simulation

- $\mu$ Lensing Event Model
- Blending Model
- Moon + Sky
- Weather
- Seeing



(Gaudi, Han, & Gould, in prep)

# DETECTING PLANETS...



13σ!!

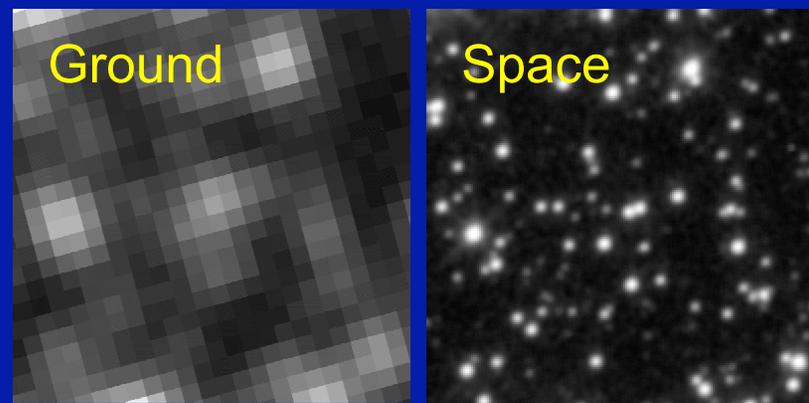
# WITH OR WITHOUT US...

- MOA-II
  - 1.8m telescope, 2.18 sq. degree camera, NZ
- OGLE -IV
  - 1.3m telescope, funding for upgrade to camera, Chile
- Proposed Initiatives
  - Korean, German, Chinese
- Pan-STARSS?
- Other Initiatives?
  - Camera for \$2 million
  - Telescope for \$5 million
- Pilot campaign this summer
  - OGLE, MOA, Wise

# WHY GROUND ISN'T GOOD ENOUGH

## Cannot yield the true potential

- MS sources severely blended
- Getting constraints on hosts is expensive
- Perturbations can be poorly sampled

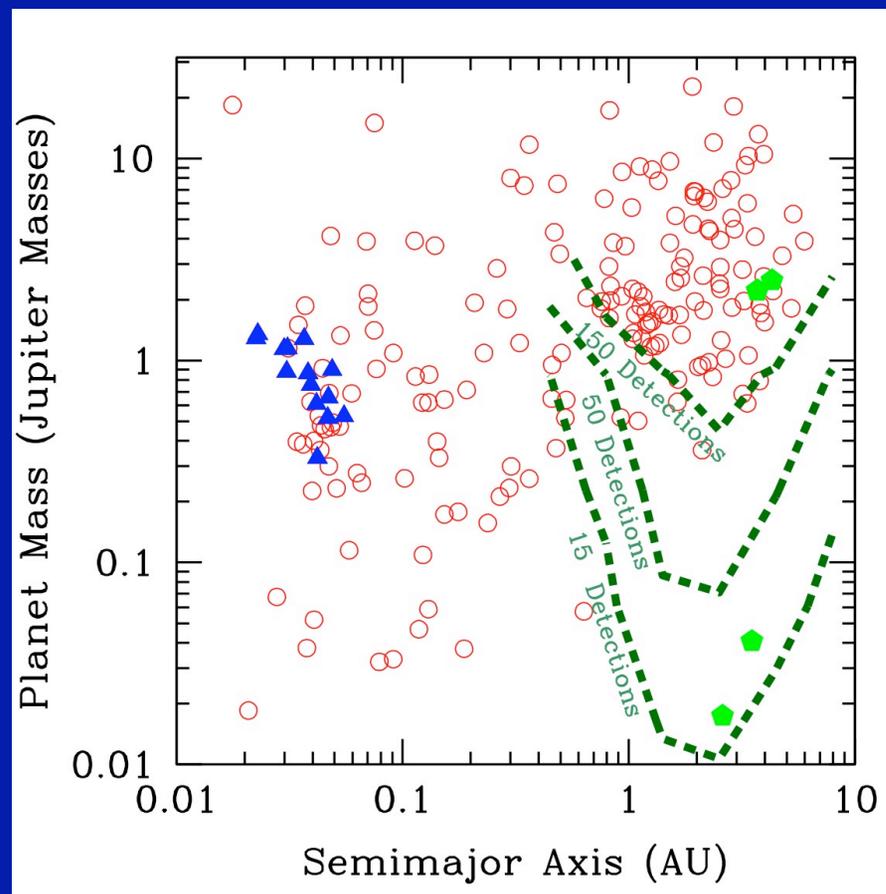


The field of microlensing event  
MACHO 96-BLG-5

# WHY GROUND ISN'T GOOD ENOUGH

Cannot yield the true potential

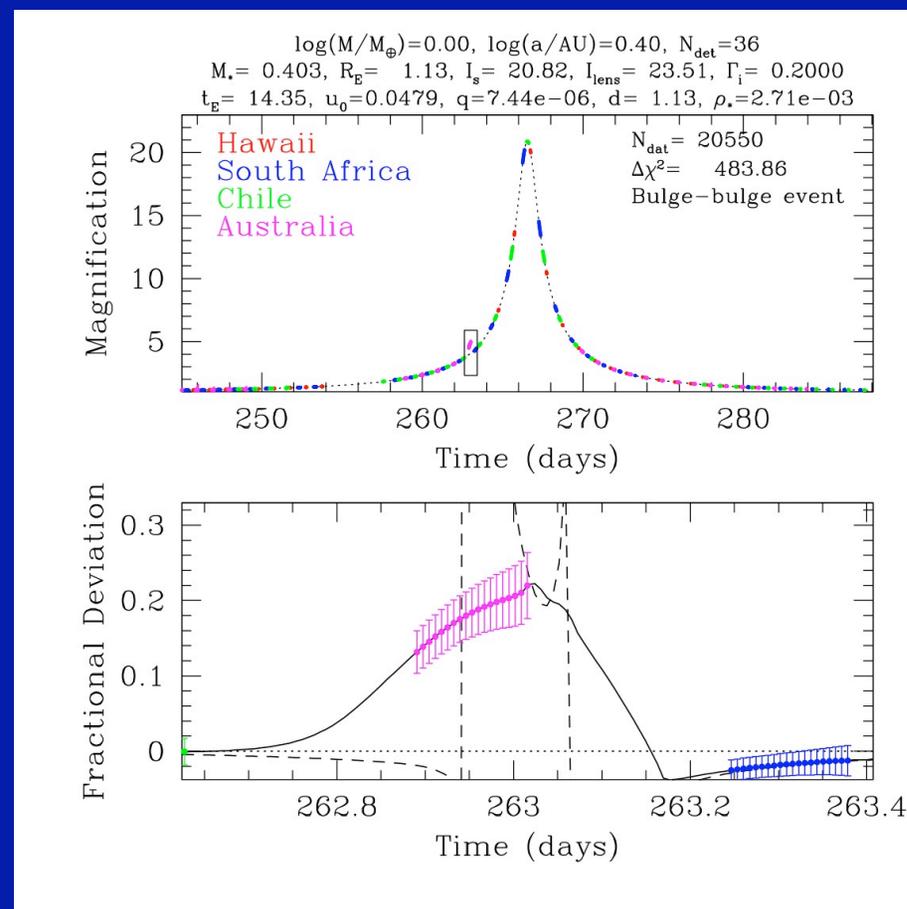
- MS sources severely blended
- Getting constraints on hosts is expensive
- Perturbations can be poorly sampled



# WHY GROUND ISN'T GOOD ENOUGH

## Cannot yield the true potential

- MS sources severely blended
- Getting constraints on hosts is expensive
- Perturbations can be poorly sampled



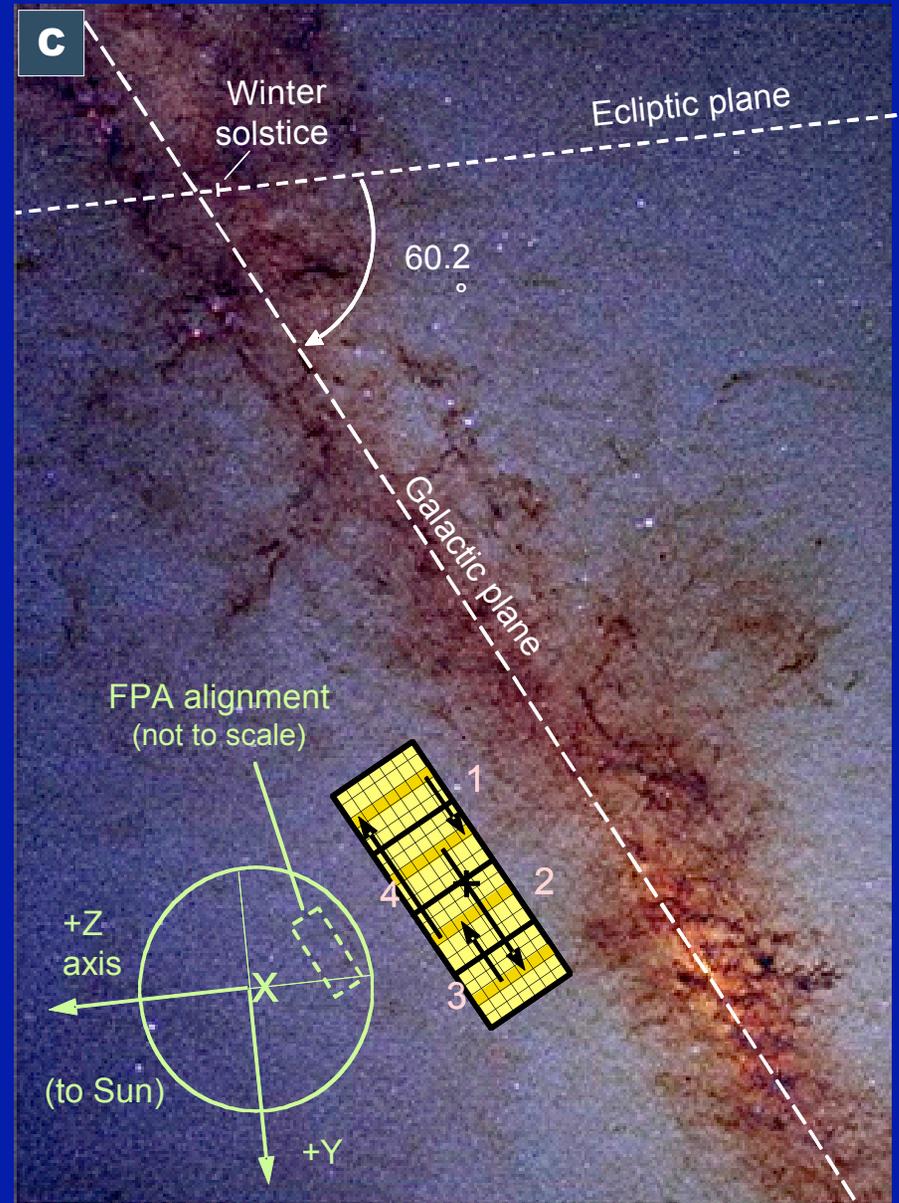
# WHAT CAN WE EXPECT FROM SPACE?

A worked example: Microlensing Planet Finder (Bennett PI)

- Simulations from Bennett & Rhie (2002) ApJ 574, 985
- Basic results confirmed by independent simulations by me
- Continuous observations of  $4 \times 0.66$  sq. deg. central Galactic bulge fields:  $\sim 2 \times 10^8$  stars
- Observations in near IR to increase sensitivity
- Simulated images based on HST luminosity function from Holtzman et al (1998)
- $\sim 15,000$  events in 4 seasons

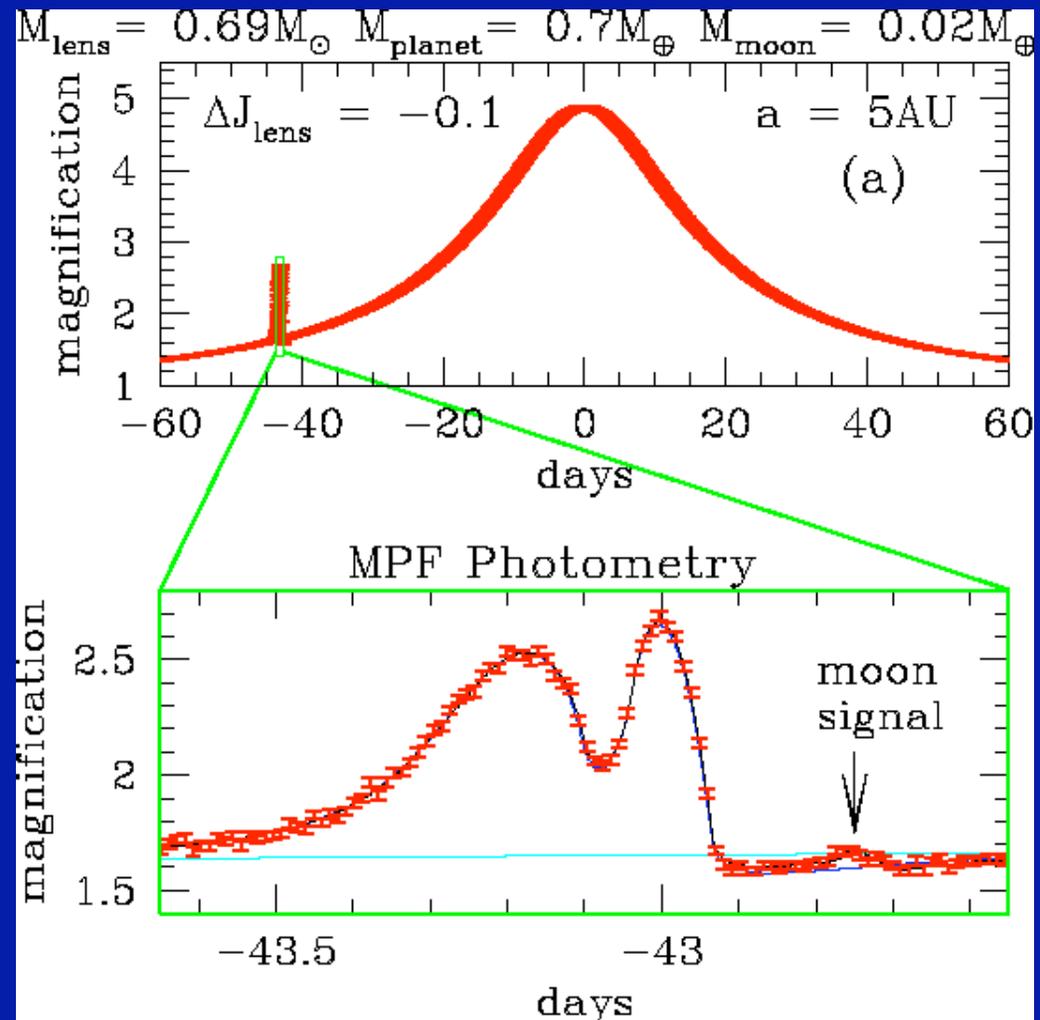
# MPF FIELDS

Four fields oriented parallel to the Galactic plane to maximize the microlensing rate.

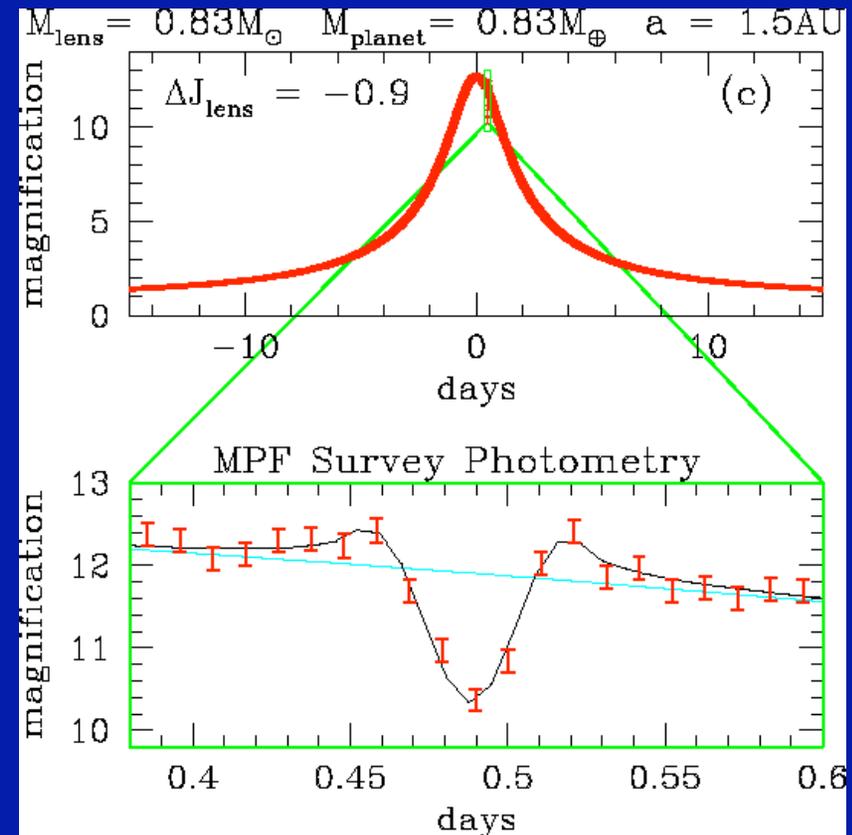
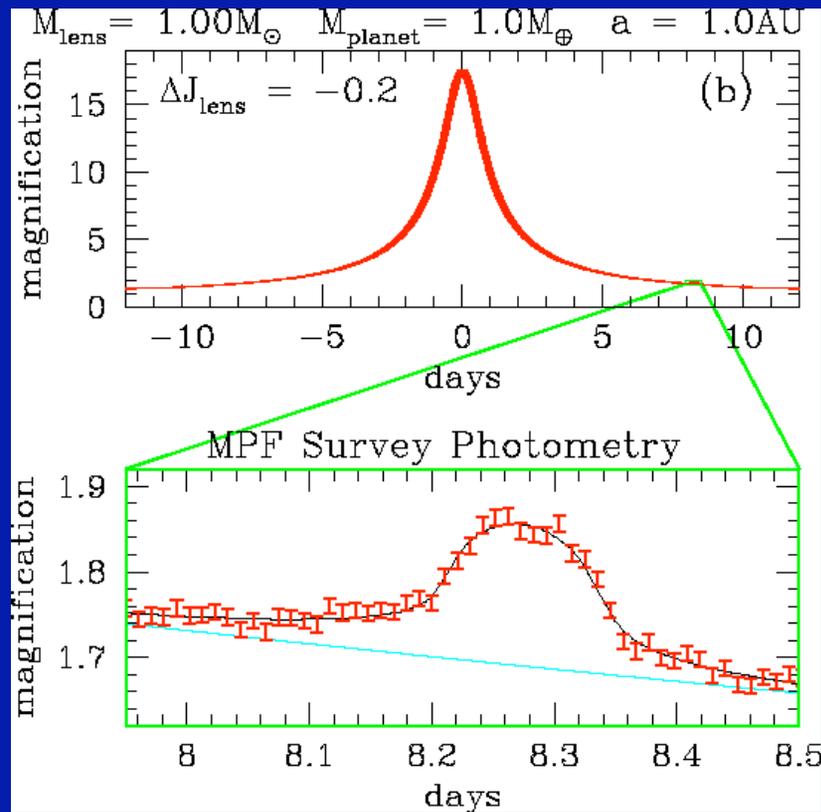


# SIMULATED PLANETARY LIGHT CURVES

- Planetary signals can be very strong
- Light curve features unambiguously yield planetary mass ratio and separation
- Exposures every 10-15 minutes
- The small deviation at day  $-42.75$  is due to a moon of 1.6 lunar masses.



# SIMULATED MPF LIGHT CURVES

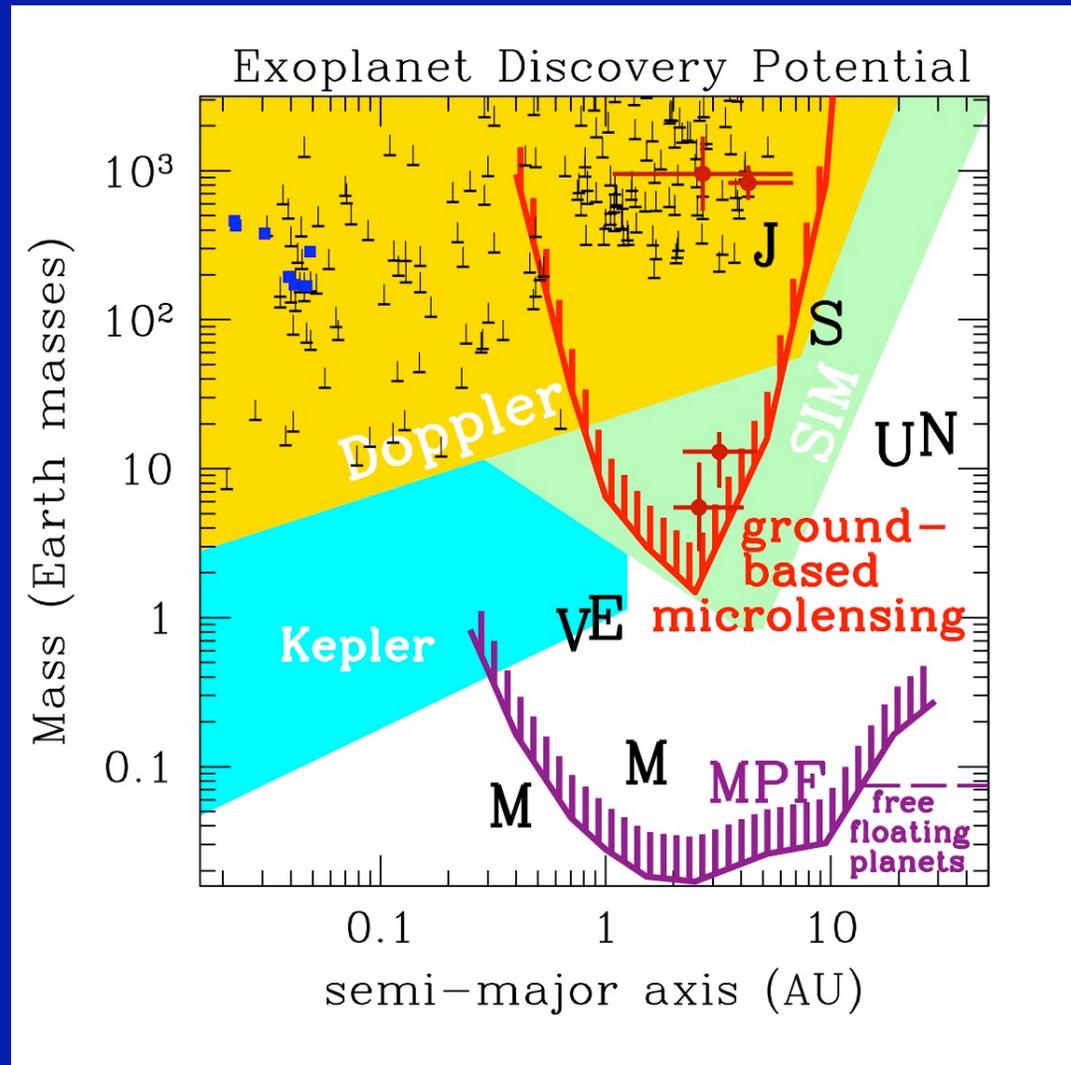


The light curves of simulated planetary microlensing events.

The lens star is brighter for each of these events.

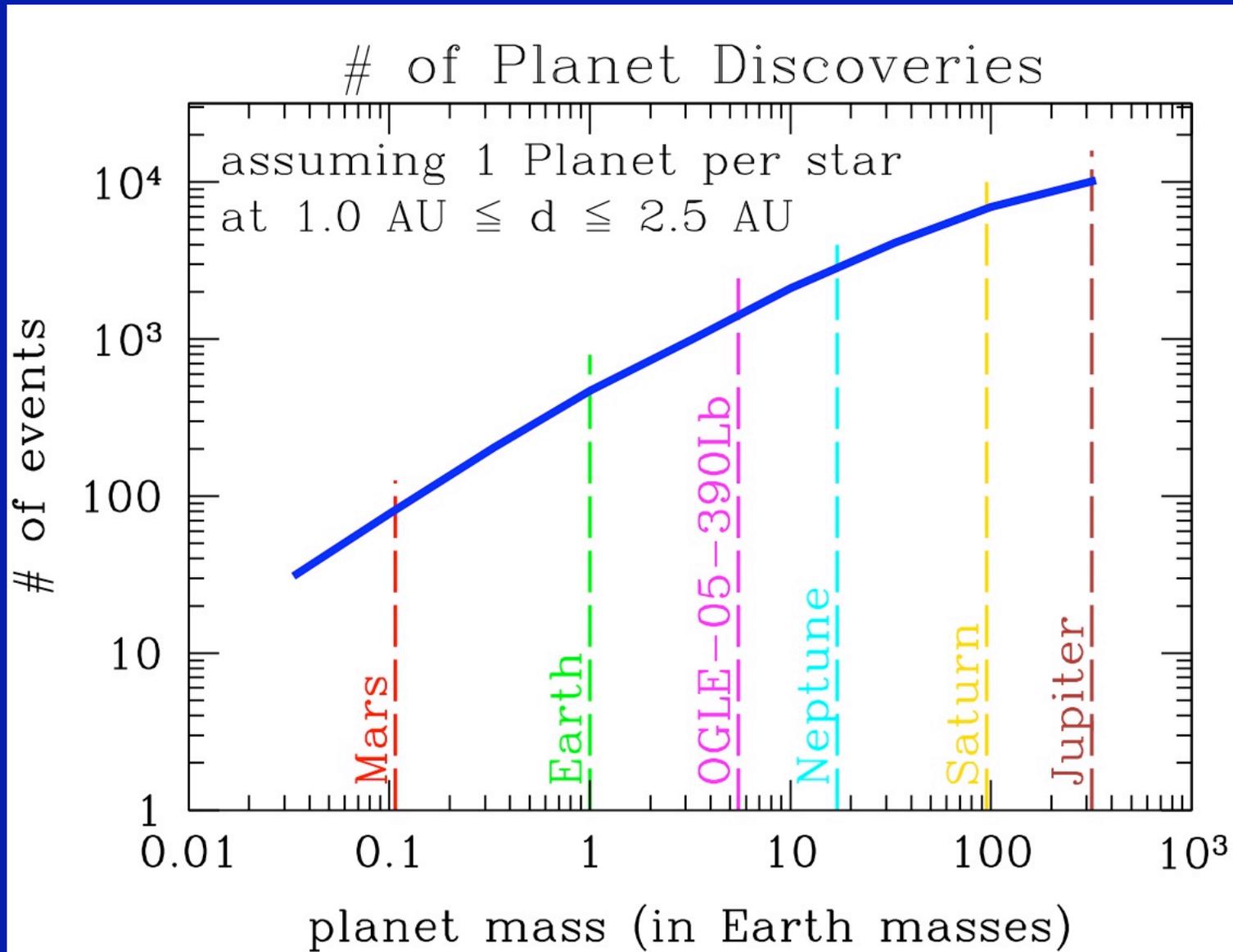
# PLANET DETECTION SENSITIVITY

- Sensitivity to all Solar System-analogs except Mercury
- most sensitive technique for  $a \geq 0.5$  AU
- Good sensitivity to “outer” habitable zone (Mars-like orbits) where detection by TPF is easiest
- Assumes  $\Delta\chi^2 \geq 80$  detection threshold
- Can find moons and free floating planets

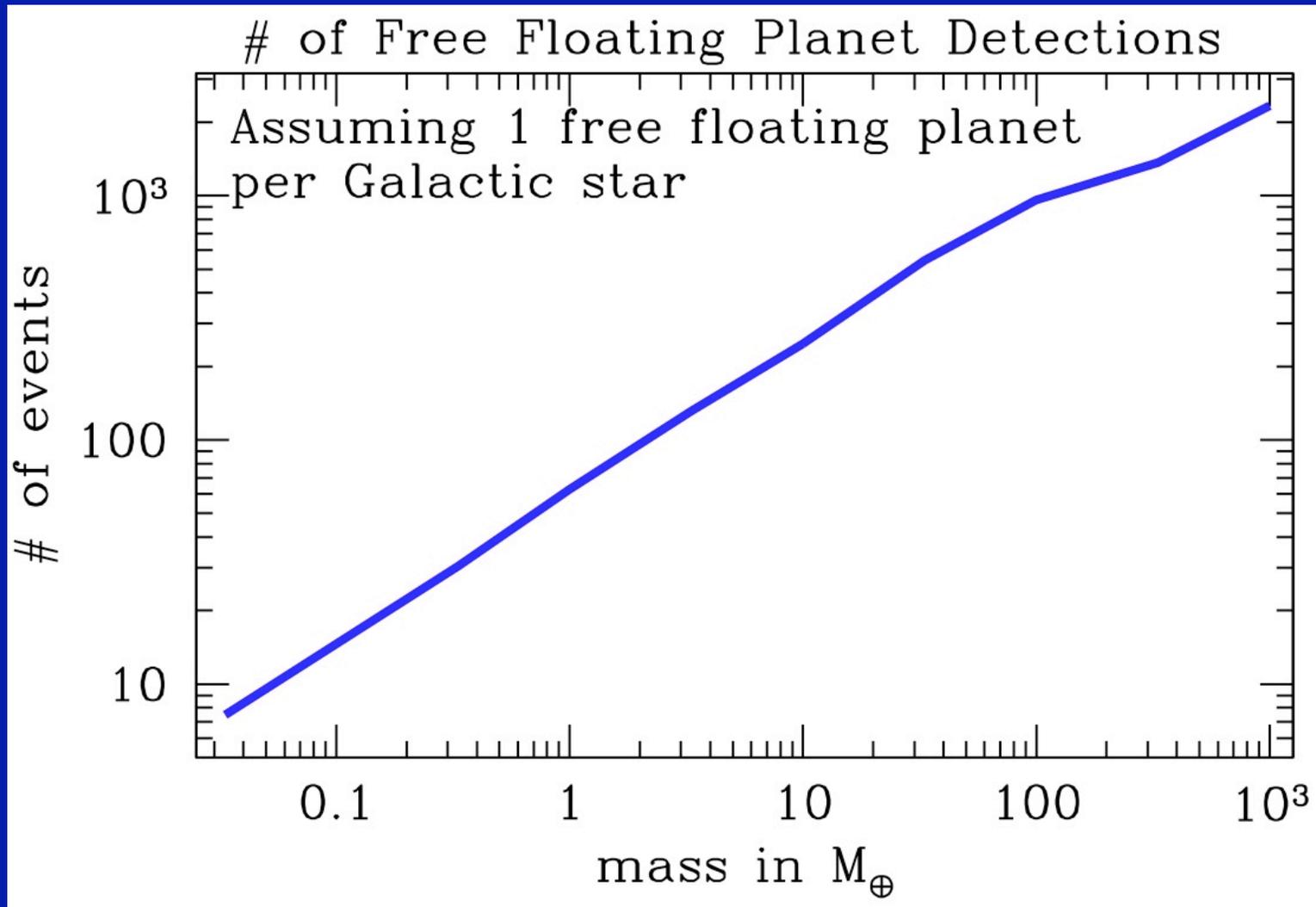


Updated from Bennett & Rhie (2002) ApJ 574, 985

# MPF DISCOVERIES

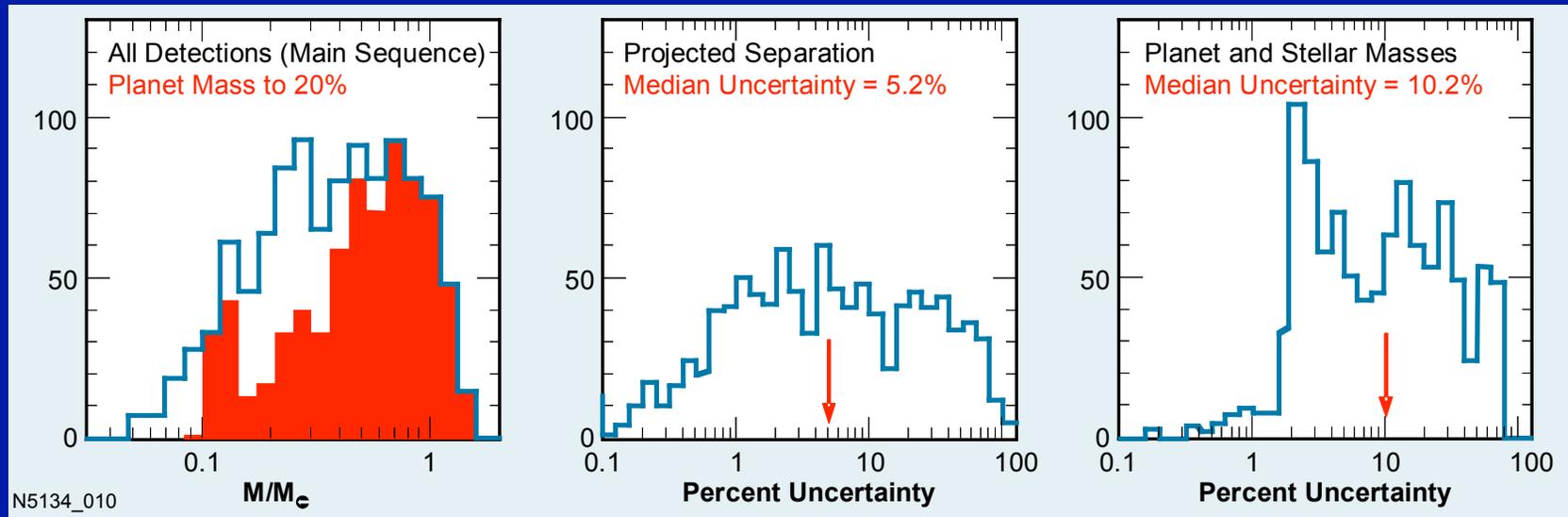


# FREE FLOATING PLANETS



Planet formation theories generically predict many free-floating planets  
(Goldreich et al. 2004, Juric & Tremaine 2007, Ford & Rasio 2007)

# LENS DETECTION PROVIDES ACCURATE MASS ESTIMATE



- Lens will be detected for the majority of main-sequence lenses.
- Host star masses will be measured to 10% for half of the event.
- Projected separations will be measured to 5% for half of the events.

# MPF WILL TELL US..

- Frequency of planets as a function of
  - mass down to  $M_{\text{mars}} = 0.1M_{\oplus}$
  - separation from  $\sim 0.5$  AU to  $\infty$
  - host star mass from  $0.1M_{\text{sun}}$  to  $1 M_{\text{sun}}$
  - Galactocentric distance from  $\sim 1$ -8 kpc (disk & bulge)
- Frequency of free-floating planets down to  $M_{\text{mars}}$
- In other words,

*MPF will tell us the frequency of almost every kind of planet that has been detected or predicted.*

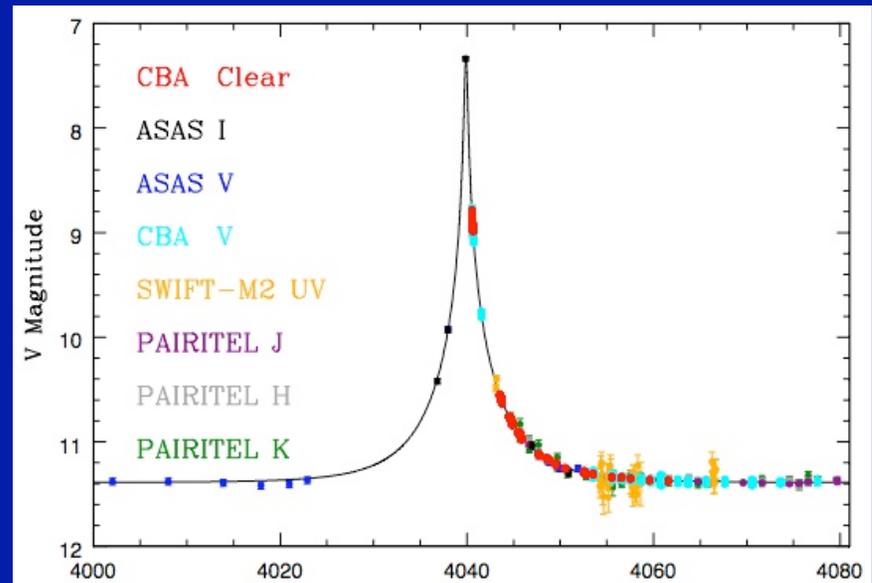
# FUTURE DIRECTIONS

## Domestic $\mu$ Lensing Events

- First event detected accidentally
- Should be 8/year within 4kpc
- Could be found with a fly's eye setup  $\sim$ \$5M

## Extragalactic Planets?

- Could be detected in M31
- Relatively minor modifications to current strategy



(Gaudi et al 2007)

# FUTURE DIRECTIONS

## Domestic $\mu$ Lensing Events

- First event detected accidentally
- Should be 8/year within 4kpc
- Could be found with a fly's eye setup  
~\$5M

## Extragalactic Planets?

- Could be detected in M31
- Relatively minor modifications to current strategy



# COST TO THE COMMUNITY

- Next generation ground-based survey
  - One telescope in South Africa would get things started
  - Cost ~\$4 M (hardware, site costs, labor)
  
- MPF fits comfortably under the Discovery cost cap ~\$400M

# A CENSUS OF PLANETARY SYSTEMS

*Understand planet formation and habitability requires a census of planets of all masses and Separations, orbiting stars of all masses.*

- Kepler will provide such a census for a  $<0.5\text{AU}$
- Microlensing is the only method that can do this for larger separations.

