

EXAM with Answers:

Course title: "Astrophysical Atomic Processes, Opacity, & Cancer Treatment with X-rays" & Computational workshops with R-matrix Codes & SUPERSTRUCTURE

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- By Sultana N. Nahar, The Ohio State University, USA

Under the MOA between Ohio State University & Cairo University

Total points = 51 (points for each question is given within parentheses)

Good luck!

1. i) What are the most abundant elements in the universe? (1)
 - H, He, Li, ..., Fe
- ii) How do the elements heavier than iron form? (1)
 - During supernova explosions, also through the s-process of neutrino capture in the stars
2. i) In what state most of the matter exists in the universe? (1)
 - In plasma state
- ii) How do we describe the distribution of electrons in plasma? (1)
 - Using Maxwellian distribution function
3. i) How do we describe the radiation from a black body? (1)
 - By Planck distribution function
- ii) What is the temperature on the surface of the sun and why do we see the yellow sun? (2)
 - Solar surface temperature is 5770 K
 - Planck function peaks at yellow wavelength on solar surface temperature or mostly yellow photons reach us
4. What is opacity? (1)
 - It is a quantity that measures the radiation absorption in the medium
5. What are the main atomic processes in astrophysical plasmas? (2.5)
 - i) Photo-excitation, ii) Photoionization, iii) Electron-ion recombination, iv) Electron-impact ionization, v) electron impact ionization
6. i) Which properties of an atom is studied under Atomic Physics? (1)
 - Electronic properties
- ii) How do we identify an element from an astrophysical spectra? (1)
 - By matching the observed spectral lines to those at the same energy positions of various known elements
- iii) How do we detect a black hole? (1)
 - By studying the spectrum of surrounding matter

iv) What happens to photons trying to escape black hole gravity? (1)

- Give out part of their energies

7. i) Write down the Rydberg formula for hydrogen lines? (1)

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$$\mathcal{E}_{n'} = \mathcal{R}_H \left[\frac{1}{n^2} - \frac{1}{n'^2} \right]$$

ii) What is the K_α line? (1)

- Absorption or emission line for 1s-2p transition

iii) What is the wavelength of Lyman α line? (1)

- 1215 Å

8. i) What is quantum defect? (1)

- It is the effect due to electron screening around nucleus of a multi-electron system

ii) Write down the Rydberg formula with the quantum defect. (1)

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$$E(nl) = \frac{z^2}{(n - \mu)^2}$$

iii) When is this formula used? (1)

- Largely for energies of excited levels

9. i) What is configuration for an atomic system? (1)

- Arrangement of electrons in the atom or ion

ii) Write down the configuration of oxygen atom with 8 electrons. (1)

- Oxygen: $1s^2 2s^2 2p^4$

iii) What quantum numbers do we use to write the symmetry of an electronic state with quantum numbers? (1)

- $(2S+1)L_J^\pi$

10. i) What are equivalent and non-equivalent states? (1)

- Equivalent: More than one electron in the outer orbital

Non-equivalent: One electron in the outer orbital

ii) Which kind has less number of LS states and why? (2)

- Equivalent electron states are less due to Pauli exclusion principle of no two electrons can have the same state

iii) Write down all the LS states of configuration $2p3d$ and list them in energy order according to Hund's rule. (3)

- $2p3d \rightarrow {}^3(F, D, P)^\circ, {}^1(F, D, P)^\circ$

iv) Write down all the LS states of configuration $2p^2$ and list them in energy order following Hund's rule. (2)

- ${}^3P, {}^1D, {}^1S$

11. i) Why do we get exact wavefunction for hydrogen, but not for multi-electron systems? (1)

- Hydrogen has one electron with central potential to the nucleus

and hence can be solved exactly for the wave function. Multi-electron system becomes complicated by angular dependence

ii) What equations do we need to solve for multi-electron systems: 1) non-relativistic, 2) relativistic approximations? (3)

- 1) Hartree-Fock equations, 2) Dirac-Fock equations or Breit-Pauli equations

iii) What approximations can we use to include relativistic effects for higher accuracy? (1)

- Dirac-Fock equation

12. i) What are the types of radiative transition we have studied? (2)

- Electric dipole, electric quadrupole, electric octupole, and magnetic dipole, magnetic quadrupole

ii) What is the name of the rules that regulate the transitions? (1)

- Selection rules

ii) What does SUPERSTRUCTURE calculate? (2)

- Wave functions, energies of the atomic system, and transition parameters - A, f, S

iii) Give an example of an allowed transition (1)

- $^3P \rightarrow ^3(S, P, D)^0$

iv) How can the lifetime of an atomic state be calculated? (1)

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$$\tau_k(\text{s}) = \frac{1}{\sum_i A_{ki}(\text{s}^{-1})}$$

13. i) What is an autoionizing state? (1)

- A doubly excited state above the ionization threshold

ii) How does it appear in a process? (0.5)

- As a resonance

14. i) What is the difference in features between hydrogenic and multi-electron photoionization? (1)

- Multi-electron systems have resonances, hydrogen does not

ii) Which approximation can calculate the resonances naturally? (1)

- Close coupling approximation

15. i) What is the relation between photoionization and electron-ion recombination? (1)

- They are inverse processes and connected by Principle of Detailed balance

ii) How many ways does electron-ion recombination take place? (1)

- Two ways: Radiative recombination, dielectronic recombination

iii) Which is the method that incorporates them together? (1)

- Unified method

16. i) What do the R-matrix codes calculate? (1)

- Quantities for atomic processes.

ii) What atomic process did you study using R-matrix codes and what quantity did you calculate? (2)

Electron impact excitation, Collision strength