



Photoionization of ground and excited levels of P II



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HIGHLIGHTS

- Presents detailed study with resonant features of photoionization of P II.
- Found prominent resonant structures and enhancement in background.
- Relativistic effect introduced important resonance at ionization threshold.
- Study considers for many excited energy levels with $n < 10$ for complete modeling.
- Relativistic Breit–Pauli R-matrix method has yielded high precision atomic data.

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ABSTRACT

Photoionization cross section (σ_{PI}) of P II, ($h\nu + \text{P II} \rightarrow \text{P III} + e$), from ground and a large number of excited levels are presented. The study includes the resonant structures and the characteristics of the background in photoionization cross sections. The present calculations were carried out in the Breit–Pauli R-matrix (BPRM) method that includes relativistic effects. The autoionizing resonances are delineated with a fine energy mesh to observe the fine structure effects. A singular resonance, formed by the coupling of channels in fine structure but not allowed in LS coupling, is seen at the ionization threshold of photoionization for the ground and many excited levels. The background cross section is seen enhanced compared to smooth decay for the excited levels. Examples are presented to illustrate the enhanced background cross sections at the energies of the core levels, $^4P_{3/2}$ and $^2D_{3/2}$, that are allowed for electric dipole transitions by the core ground level $^2P_{1/2}$. In addition strong Seaton or photo-excitation-of-core (PEC) resonances are found in the photoionization of single valence electron excited levels. Calculations used a close coupling wave function expansion that included 18 fine structure levels of core P III from configurations $3s^23p$, $3s3p^2$, $3s^23d$, $3s^24s$, $3s^24p$ and $3p^3$. Photoionization cross sections are presented for all 475 fine structure levels of P II found with $n \leq 10$ and $l \leq 9$. The present results will provide high precision parameters of various applications involving this less studied ion.

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1. Introduction

Phosphorus is part of our daily life in variety of applications. Being an element of RNA where it plays a role in signal passing, it is also a basic element like carbon, oxygen in the evolution of life. However, its astrophysical abundance is low and is difficult to detect due to lack of data. Its existence in astronomical objects has been found in damp Galaxies by Molaro et al. (2001) and by Welsh et al. (2001). Compared to other elements, only very limited theoretical study has been carried out on the radiative processes of this element.

Photoionization cross sections of Si-like ions, isoelectronic to P II, have been reported under the (OP, 1996) by Mendoza and Zeppen (1988); Nahar and Pradhan (1993). However, P which is the next element to Si in the periodic table, was not studied due to lower abundance in astrophysical plasmas. Photoionization cross section of P II has been measured recently with high precision at the Advanced Light Source (ALS) by Hinojosa et al. (2015) where they studied the low energy features in detail. The observed features were identified theoretically using R-matrix method and were found to be produced by low lying fine structure levels that belong to ground configuration $3s^23p^2$ and one metastable state $3s3p^3(^5S_2^o)$. The present work reports full scale study of features of photoionization, such as, background enhancement, photo-excitation-of core resonances, and reporting cross sections of a large number of excited levels, 475 in total with $n \leq 10$ as needed for spectral modelings. In contrast to the study of photoionization

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of Si-like ions in non-relativistic LS coupling (Nahar and Pradhan, 1993), the present study employed the Breit-Pauli R-matrix (BPRM) method with relativistic effects developed under the Iron Project Hummer et al. and includes radiation damping effect of resonances (Zhang et al., 1999).

2. Theory

Photoionization process can be direct as,

$$h\nu + X^+ \rightarrow e + X^{2+}. \quad (1)$$

However, depending on the photon energy which matches the energy of a state belonging to Rydberg series of states below an excited core state but lying above the ionization threshold, an intermediate doubly excited autoionizing state can form before ionization,

$$h\nu + X^+ \rightleftharpoons (X^+)^{**} \rightleftharpoons e + X^{2+} \quad (2)$$

Formation of an autoionizing state can lead to a resonance in photoionization and is the main cause for introduction of features and structures in the process.

Theoretically the resonances can be generated naturally in an ab initio manner by including the core excitations in the wave function, as considered in the close coupling (CC) approximation. In CC approximation, the atomic system is represented by a (N+1) number of electrons where the core ion is an N-electrons system interacting with the (N+1)th electron. The (N+1)th electron can be bound or in the continuum depending on its negative or positive energy (E). The total wave function, Ψ_E , in a symmetry $SL\pi$ of the system is expressed by an expansion as (e.g. Pradhan and Nahar, 2011)

$$\Psi_E(e + ion) = A \sum_i \chi_i(ion)\theta_i + \sum_j c_j \Phi_j, \quad (3)$$

where χ_i is the core ion eigenfunction representing ground and various excited states and the sum is over the number of core states considered. The core is coupled with the (N+1)th electron function, θ_i . The (N+1)th electron with kinetic energy k_i^2 is in a channel labeled as $S_i L_i (J_i) \pi_i k_i^2 \ell_i [SL(J)\pi]$. A is the antisymmetrization operator. In the second sum, the Φ_j s are bound channel functions of the (N+1)-electrons system that provides the orthogonality between the continuum and the bound electron orbitals and account for short range correlation. Substitution of $\Psi_E(e + ion)$ in the Schrodinger equation

$$H_{N+1}^{BP} \Psi_E = E \Psi_E \quad (4)$$

introduces a set of coupled equations that are solved using the R-matrix approach. The details of the R-matrix method in the CC approximation can be found in, e.g. (Burke and Robb, 1975; Seaton, 1987; Berrington et al., 1987; 1995; Pradhan and Nahar, 2011). The relativistic effects are included through Breit-Pauli approximation (e.g. Pradhan and Nahar, 2011) where the Hamiltonian is given by

$$H_{N+1}^{BP} = \sum_{i=1}^{N+1} \left\{ -\nabla_i^2 - \frac{2Z}{r_i} + \sum_{j>i}^{N+1} \frac{2}{r_{ij}} \right\} + H_{N+1}^{mass} + H_{N+1}^{Dar} + H_{N+1}^{so}, \quad (5)$$

in Rydberg unit. The relativistic correction terms are mass correction, $H^{mass} = -\frac{\alpha^2}{4} \sum_i p_i^4$, Darwin, $H^{Dar} = \frac{Z\alpha^2}{4} \sum_i \nabla^2(\frac{1}{r_i})$, and spin-orbit interaction, $H^{so} = Z\alpha^2 \sum_i \frac{1}{r_i^3} \mathbf{l}_i \cdot \mathbf{s}_i$. R-matrix Breit-Pauli (BPRM) approximation also includes part of two-body interaction terms, such as the ones without the momentum operators (Pradhan and Nahar, 2011). In BPRM method the set of $SL\pi$ is recoupled for $J\pi$

Table 1

Levels and energies (E_i) of core ion P III included in the wave function expansion of P II. Calculated energies from SUPERSTRUCTURE (SS) are compared with those in the compiled table of NIST.

Level		J_i	E_i (Ry) NIST	E_i (Ry) SS
1	$3s^2 3p(^2P^o)$	1/2	0.0	0.
2	$3s^2 3p(^2P^o)$	3/2	0.005095	0.00429
3	$3s 3p^2(^4P)$	5/2	0.523559	0.51278
4	$3s 3p^2(^4P)$	3/2	0.520570	0.51028
5	$3s 3p^2(^4P)$	1/2	0.518708	0.50874
6	$3s 3p^2(^2D)$	3/2	0.682693	0.70551
7	$3s 3p^2(^2D)$	5/2	0.682957	0.70565
8	$3s 3p^2(^2S)$	1/2	0.913094	0.99414
9	$3s 3p^2(^2P)$	1/2	0.993621	1.03335
10	$3s 3p^2(^2P)$	3/2	0.997044	1.03613
11	$3s^2 3d(^2D)$	3/2	1.065039	1.14381
12	$3s^2 3d(^2D)$	5/2	1.065142	1.14392
13	$3s^2 4s(^2S)$	1/2	1.073800	1.10909
14	$3s^2 4p(^2P^o)$	1/2	1.28832	1.34867
15	$3s^2 4p(^2P^o)$	3/2	1.28956	1.34955
16	$3p^3(^2D^o)$	3/2	1.342508	1.38637
17	$3p^3(^2D^o)$	5/2	1.343073	1.38678
18	$3p^3(^4S^o)$	3/2	1.455433	1.49071

levels of (e + ion) system in intermediate coupling which is followed by diagonalization of the Hamiltonian.

For an electron with positive energies ($E > 0$) the solution of the BPRM method is a continuum wave function, Ψ_F and with negative energy ($E \leq 0$) it is a bound state, Ψ_B . The complex resonant structures in photoionization are produced from couplings between continuum channels that are open ($k_i^2 > 0$), and bound channels that are closed ($k_i^2 < 0$), at electron energies k_i^2 which correspond to autoionizing states of the Rydberg series, $S_i L_i J_i \pi_i \nu \ell$, where ν is the effective quantum number of the series converging to excited core thresholds $S_i L_i J_i \pi_i$.

The photoionization cross section (σ_{PI}) is given by (e.g. Pradhan and Nahar, 2011)

$$\sigma_{PI} = \frac{4\pi^2}{3c} \frac{1}{g_i} \omega \mathbf{S}, \quad (6)$$

where g_i is the statistical weight factor of the bound state, ω is the incident photon energy and \mathbf{S} is the generalized line strength

$$\mathbf{S} = |\langle \Psi_f || \mathbf{D}_L || \Psi_i \rangle|^2 = \left| \left\langle \Psi_f \left| \sum_{j=1}^{N+1} r_j \right| \Psi_i \right\rangle \right|^2, \quad (7)$$

where Ψ_i and Ψ_f are the initial and final state wave functions, and \mathbf{D}_L is the dipole operator in length form.

3. Computations

BPRM computations are carried out using the R-matrix package of codes (Berrington et al., 1995; Nahar and Pradhan, 1994; Zhang et al., 1999) for various stages. They are initiated with the wave function of the core as the initial input. The core wave function for P III was obtained from atomic structure calculations using code SUPERSTRUCTURE (SS) (Eissner et al., 1974; Nahar et al., 2003). SS uses Thomas-Fermi-Dirac-Amaldi potential and includes relativistic contributions in Breit-Pauli approximation. Table 1 presents ground and 17 excited fine structure levels of P III included in the wave function expansion of P II. They were obtained from optimization of 19 configurations up to 5s orbital of P III, $3s^2 3p(1)$, $3s 3p^2(2)$, $3s^2 3d(3)$, $3s^2 4s(4)$, $3s^2 4p(5)$, $3p^3(6)$, $3s 3p 3d(7)$, $3s^2 4d(8)$, $3s^2 4f(9)$, $3s^2 5s(10)$, $3s 3p 4s(11)$, $3s 3p 4p(12)$, $3s 3p 4d(13)$, $3s 3p 4f(14)$, $3p^2 3d(15)$, $3p^2 4s(16)$, $3p^2 4p(17)$, $3p^2 4d(18)$, $3p^2 4f(19)$. The calculated energies from SS are compared with observed values (listed

at NIST from compilation by Martin et al., 1985) in the table. Comparison shows agreement between SS and observed values within a few percent mostly. For accurate energy positions of the resonances the calculated core P III were replaced by the observed energies listed at NIST website, during diagonalization of the $(N+1)$ -electron Hamiltonian.

The wave function of P II included $0 \leq \ell \leq 10$ partial waves for the interacting electron and 16 continuum functions for the R-matrix basis sets. The R-matrix boundary was chosen to be large enough, $15 a_0$, to accommodate the bound orbitals. The second term of the wave function, which represents the bound state correlation functions, included 39 $(N+1)$ -particle configurations with orbital occupancies from minimum to a maximum number as given within parentheses of the orbitals $1s(2-2)$, $2s(2-2)$, $2p(6-6)$, $3s(0-2)$, $3p(0-4)$, $3d(0-3)$, $4s(0-2)$, $4p(0-2)$, $4d(0-2)$, $4f(0-1)$, $5s(0-1)$.

Photoionization cross sections are obtained with consideration of radiation damping for all bound levels using the BPRM R-matrix codes (Berrington et al., 1995; Zhang et al., 1999). The narrow resonances of photoionization were delineated at a very fine energy mesh.

4. Results and discussions

Detailed study of photoionization cross sections (σ_{PI}) of Si-like phosphorus ion, P II, are presented. As a basic element of evolution of life, it is important to study the features to help in identifying this element in astrophysical and laboratory plasmas. A total of 475 bound levels of P II with $n \leq 10$, $0 \leq l \leq 9$, $0 \leq J \leq 7$ of even and odd parities were found. They have been identified spectroscopically using the theoretical procedure based on the quantum defect analysis, percentage of channels contribution, and angular momenta algebra (Nahar and Pradhan, 2000, Nahar 2013). A sample table of energy comparison is given in Table 2 and the complete table will be available electronically from database NORAD-Atomic-Data. Photoionization cross sections of all 475 bound fine structure levels of P II are presented. This will enable complete modelings, such as, of plasma opacities, synthetic spectrum, and diagnostics. Examples of σ_{PI} illustrating important characteristic features are discussed below.

Table 2

Comparison between calculated BPRM and compiled energies by Martin et al. (1985) (listed at NIST website NIST) of P II. J_l is the calculated level index for its position in its $J\pi$ symmetry. Negative sign for energies omitted for convenience.

Level	$J : J_l$	$E(\text{Ry}, \text{BPRM})$	$E(\text{Ry}, \text{NIST})$
$3s^2 3p^2$	$^3P^e$ 2 : 1	1.4539E+00	1.4799E+00
$3s^2 3p^2$	$^3P^e$ 1 : 1	1.4566E+00	1.4824E+00
$3s^2 3p^2$	$^3P^e$ 0 : 1	1.4581E+00	1.4838E+00
$3s^2 3p^2$	$^1D^e$ 2 : 2	1.3772E+00	1.3982E+00
$3s^2 3p^2$	$^1S^e$ 0 : 2	1.2615E+00	1.2568E+00
$3s3p^3$	$^5S^o$ 2 : 1	1.0417E+00	1.0601E+00
$3s3p^3$	$^3D^o$ 3 : 1	8.6300E-01	8.6413E-01
$3s3p^3$	$^3D^o$ 2 : 2	8.6332E-01	8.6453E-01
$3s3p^3$	$^3D^o$ 1 : 1	8.6351E-01	8.6477E-01
$3s3p^3$	$^3P^o$ 2 : 3	7.5860E-01	7.3613E-01
$3s3p^3$	$^3P^o$ 1 : 2	7.5816E-01	7.3487E-01
$3s3p^3$	$^3P^o$ 0 : 1	7.5806E-01	7.3469E-01
$3s^2 3p3d$	$^1D^o$ 2 : 4	7.4998E-01	7.3226E-01
$3s^2 3p4s$	$^3P^o$ 2 : 5	6.6419E-01	6.5189E-01
$3s^2 3p4s$	$^3P^o$ 1 : 3	6.6765E-01	6.5504E-01
$3s^2 3p4s$	$^3P^o$ 0 : 2	6.6899E-01	6.5636E-01
$3s^2 3p3d$	$^3P^o$ 4 : 1	6.5446E-01	6.2050E-01
$3s^2 3p3d$	$^3P^o$ 3 : 2	6.5651E-01	6.2265E-01
$3s^2 3p3d$	$^3P^o$ 2 : 6	6.5799E-01	6.2423E-01
$3s^2 3p4s$	$^1P^o$ 1 : 4	6.4807E-01	6.2961E-01

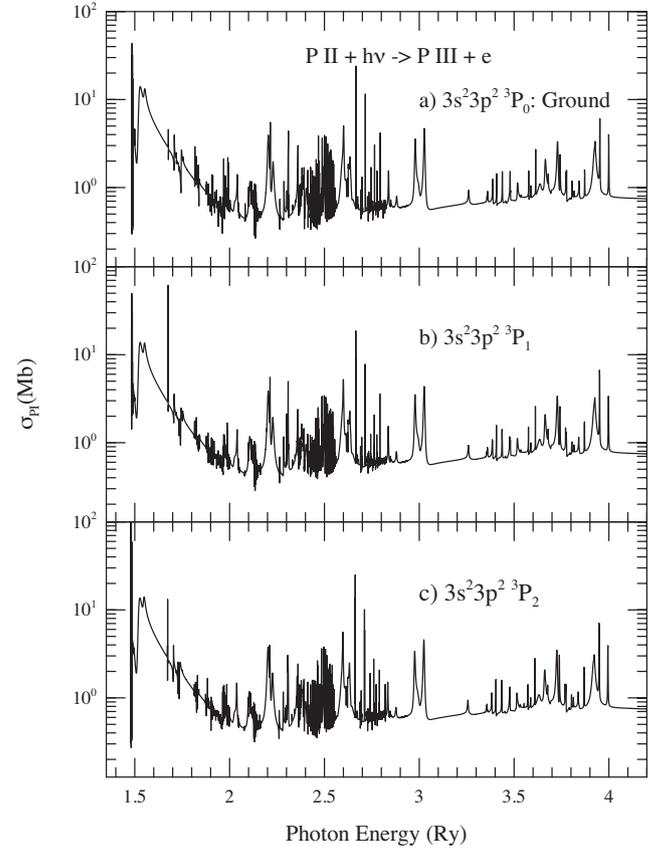


Fig. 1. Photoionization cross sections, σ_{PI} , of the ground 3P_0 (a) and two excited, $^3P_{1,2}$ (b,c) levels of the ground configuration $3s^2 3p^2$ of P II. The sharp resonance at the threshold is due to coupling of fine structure channels.

Photoionization cross sections of the ground, 3P_0 and two excited, $^3P_{1,2}$ levels of the ground configuration $3s^2 3p^2$ of P II are presented in Fig. 1. They look similar, except some resonances, as the levels belong to the same state 3P . Each level shows existence of narrow resonance at the ionization threshold followed by a prominent broad resonant structure. These indicate high rate for ionization at low energy and the inverse process of recombination at low temperature supporting high reactivity of this low charge ion. The broad structure is very much similar to that found in photoionization of 3P ground state of Si I in Fig. 1 of (Nahar and Pradhan, 1993). Si I is isoelectronic to P II and the element before P in the periodic table. However, the narrow resonance appearing at ionization threshold in P II is missing in σ_{PI} of Si I. Calculations for Si I were carried out in non-relativistic LS coupling approximation and these resonances were not allowed in the approximation. The ground state $3s^2 3p^2(^3P)$ can photoionize to the three allowed states, $^3S^o$, $^3P^o$, $^3D^o$. The broad structure can be explained as the combination of autoionizing states that belong to the Rydberg series of states $3s3p^2(^4P)\nu l(^3S^o, ^3P^o, ^3D^o)$ converging on to excited core state $3s3p^2(^4P)$. LS coupling does not allow the excitation of the fine structure level $2p(^2P^o_{3/2})$. Inclusion of relativistic effects for P II has allowed channels $2p(^2P^o_{3/2})\nu s_{1/2}$ and $2p(^2P^o_{3/2})\nu d_{3/2,5/2}$ to form $^3S^o$, $^3P^o$, $^3D^o$ levels, and hence the autoionizing resonance at the threshold. Relativistic effects are not important in general for low charged ions, such as, P II, but can introduce important sharp resonances in the low energy region.

Various features in photoionization of the ground level can be interpreted through the partial photoionization cross sections of the level leaving the residual ion in different core states. Fig. 2

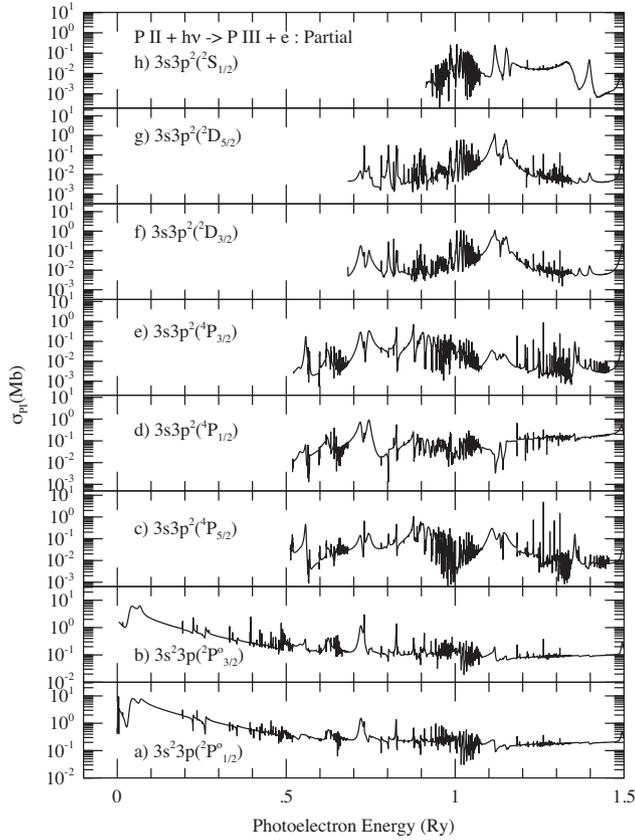


Fig. 2. Partial photoionization cross sections, σ_{PI} , of the ground 3P_0 level of P II leaving the core in the ground (a) and next seven excited levels, $3s^2 3p(2P_{3/2}^o)$, $3s^2 3p(4P_{1/2, 3/2, 5/2}, 2D_{3/2, 5/2}, 2S_{1/2})$ (b-h) of core P III.

presents partial cross sections of ground level 3P_0 of P II leaving the core ion in the ground $3s^2 3p(2P_{1/2}^o)$ and next seven excited $3s^2 3p(2P_{3/2}^o)$, $3s^2 3p(4P_{1/2, 3/2, 5/2}, 2D_{3/2, 5/2}, 2S_{1/2})$ levels of P III (listed in Table 1). Panel (a) which presents partial σ_{PI} for leaving the core at the ground level $3s^2 3p(2P_{1/2}^o)$ illustrates that the narrow resonance at threshold belongs to Rydberg series of $3s^2 3p(2P_{3/2}^o)\nu l$ where ν is the effective quantum number. There is no fine structure splitting of $2P^o$ in LS coupling and hence no such resonance can be formed. However, this resonance appears naturally in photoionization of P II as reported in Hinojosa et al. (2015). Panels (c,f and g) which present partial σ_{PI} leaving the core at states $3s^2 3p(4P_{5/2}, 2D_{3/2, 5/2})$ show that the enhanced resonant structure with peaks at about 1.15 Ry of photoelectron energy have appeared as the enhanced background at about 2.65 Ry in the cross sections of $^3P_{0, 1, 2}$ in Fig. 1.

The threshold resonance due to fine structure couplings of channels for the ground level of P II is found to exist in other equivalent states of P II. Fig. 3 shows this resonance appearing in σ_{PI} of the three levels of equivalent state, $3s^2 3p(3D_{1,2,3}^o)$. This relativistic effect is compared with the non-relativistic LS coupling photoionization cross sections of $3s^2 3p(3D^o)$ state of Si I which is isoelectronic to P II (Nahar and Pradhan, 1993). As in the case of the ground state, σ_{PI} of Si I does not show the existence of this resonances since it is not allowed in LS coupling. This resonance should give important contribution in photoabsorption at low temperature plasma. It may be noted that P II shows more resonances compared to Si I. This can be explained by the fine structure splitting of the core states and thus introducing more Rydberg series of autoionizing resonances in relativistic calculations. The other im-

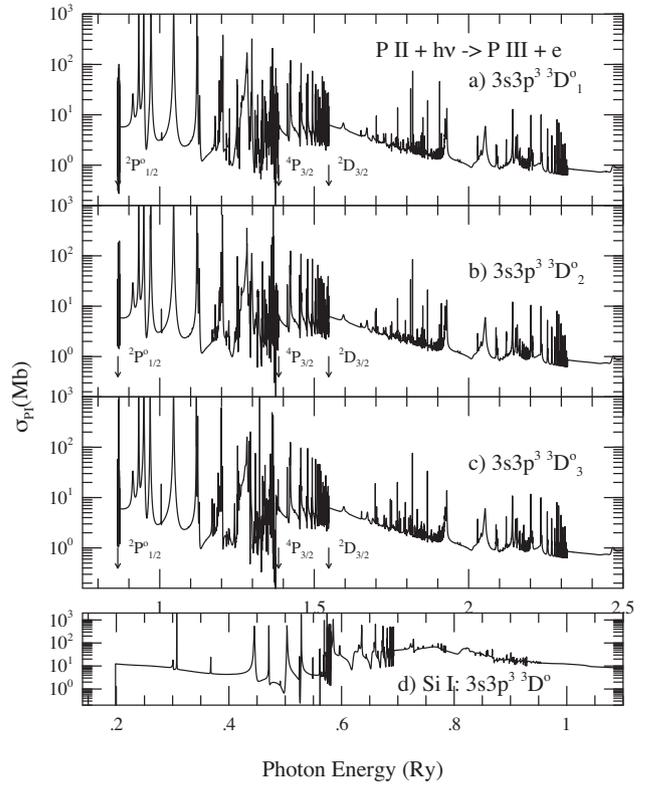


Fig. 3. Photoionization cross sections, σ_{PI} , of the three levels of equivalent state, $3s^2 3p(3D_{1,2,3}^o)$ (a-c) of P II. Relativistic fine structure effect is illustrated in producing i) the narrow and sharp resonance at the threshold and ii) enhancing the background cross section at energies 1.3845 and 1.547 Ry (pointed by arrows) due to the allowed dipole transitions of the core ground level $3s^2 3p(2P_{1/2}^o)$ to excited levels $3s^2 3p(4P_{3/2}, 3s^2 3p(2D_{3/2})$. The effects are compared with σ_{PI} of isoelectronic element Si I (d) for which there is no threshold resonance due to its no consideration of relativistic effects.

portant feature to note in σ_{PI} of these levels is the prominent enhancement in the background cross sections at two energies, as pointed by arrows in the plots, the first one at about 1.3845 Ry, which is sum of ionization potential 0.864 Ry and core excitation energy 0.521 Ry for level $3s^2 3p(4P_{3/2})$, and the second one at about 1.547 Ry, which is sum of the ionization energy 0.864 Ry and core excitation energy of 0.683 Ry of level $3s^2 3p(2D_{3/2})$. Both $3s^2 3p(4P_{3/2})$ and $3s^2 3p(2D_{3/2})$ are allowed by strong dipole transition from the core ground level $3s^2 3p(2P_{1/2}^o)$ causing the enhancement. The high energy σ_{PI} of levels of $3D^o$ appear to be decaying faster than that of isoelectronic Si I. The possible reason could be the charge of P II which is following the $1/z^2$ rule for the background cross section where z is the charge of the ion.

The other prominent feature in photoionization is the existence of Seaton or photo-excitation-of-core (PEC) resonances (e.g. Pradhan and Nahar, 2011) in excited levels with a single valence electron. Here the outer electron remains as a spectator while the core absorbs the photon for a dipole allowed transition from the ground level which is then followed by photoionization as the core drops down to ground level. Hence regardless of the ionization potential of the excited level these resonances appear at the same energy positions when the photon absorption matches to that of the core excitation. Fig. 4 illustrates these Seaton (who explained it in Yu and Seaton (1987) for the first time) or PEC resonances for photoionization of three excited levels, $3s^2 3p6p(3P_0)$ (a), $3s^2 3p4p(3D_2)$ (b) and $3s^2 3p5d(3D_2^o)$ (c) of P II. The figure demonstrates the importance of these resonances, positions are pointed by arrows, for

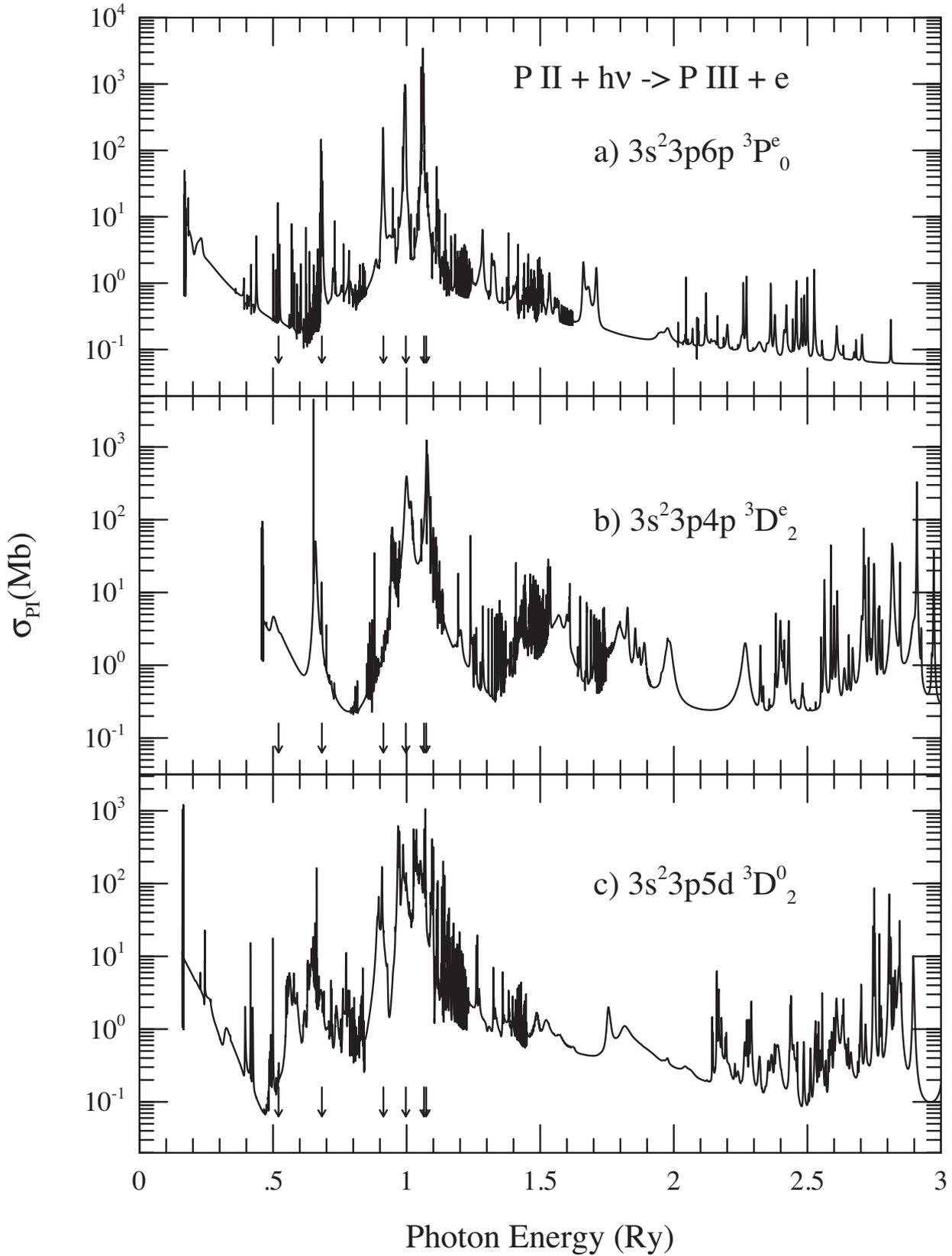


Fig. 4. Photoionization cross sections, σ_{PI} , of three excited levels, $3s^2 3p 6p(^3P_0)$ (a), $3s^2 3p 4p(^3D_2)$ (b) and $3s^2 3p 5d(^3D_2^0)$ (c) of P II illustrating photo-excitation-of-core (PEC) or Seaton resonances which occur at the excitation energies of the core as pointed out by the arrows. It can be seen that core excitations not only introduced sharp resonances, they enhanced the background by orders of magnitude.

Table 3

Possible dipole allowed transitions from the ground level $3s^2 3p(^2P_{1/2}^o)$ to various excited levels of core P III for introduction of Seaton or PEC resonances. The level number corresponds to that of Table 2.

Level numbers	Core transition	E(Ry) position	Level numbers	Core transition	E(Ry) position
1-4	$3s^2 3p(^2P_{1/2}^o) - 3s3p^2(^4P_{1/2})$	0.5187	1-9	$3s^2 3p(^2P_{1/2}^o) - 3s3p^2(^2P_{1/2})$	0.9936
1-5	$3s^2 3p(^2P_{1/2}^o) - 3s3p^2(^4P_{3/2})$	0.5206	1-10	$3s^2 3p(^2P_{1/2}^o) - 3s3p^2(^2P_{3/2})$	0.9970
1-6	$3s^2 3p(^2P_{1/2}^o) - 3s3p^2(^2D_{3/2})$	0.6827	1-11	$3s^2 3p(^2P_{1/2}^o) - 3s^2 3d(^2P_{3/2})$	1.065
1-8	$3s^2 3p(^2P_{1/2}^o) - 3s3p^2(^2S_{1/2})$	0.9131	1-13	$3s^2 3p(^2P_{1/2}^o) - 3s^2 4s(^2S_{1/2})$	1.073

excited levels which are often treated as hydrogenic. The core excitations to dipole allowed levels introduce not only sharp peak, can also enhance the background considerably, by orders of magnitude as can be seen for the four PEC positions around 1 Ry. Table 3 lists the core excitations for possible formation of Seaton resonances and their energy positions. As the table shows, there are several excited levels around 1 Ry for dipole allowed transitions of the core. It may be noted in the figure that each level is also showing threshold resonance.

5. Conclusion

Photoionization of ($h\nu + \text{P II} \rightarrow e + \text{P III}$) is studied in detail with emphasis on the resonant and background features. Of particular interest is the sharp resonance at the ionization threshold due to relativistic effects, but not possible in LS coupling, for many levels. This may have important impact on the recombination rates, photoionization rates at low temperature. Enhancement has been found at excited core thresholds. The cross sections of excited levels of single valence electrons show dominance of Seaton resonances over the background. The prominent features are expected to contribute considerably in various laboratory and astrophysical models. The present work reports photoionization cross sections of a large set, 475 in total, levels with $n \leq 10$ and $l \leq 9$ and $0 \leq J \leq 7$ of even and odd parities. Based on the accuracy of the wave function expansion, R-matrix method with inclusion of relativistic effects, and very good agreement with experiment (Hinojosa et al., 2015), the accuracy of the presented cross sections is estimated to be 15–20 % and the amount of data are expected to provide a complete and precise modeling for various applications.

The complete set of data for photoionization cross sections and the energy levels are available on-line from NORAD-Atomic-Data website at: <http://norad.astronomy.ohio-state.edu/>.

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